

FLUID + JET

Yasuki Tachibana

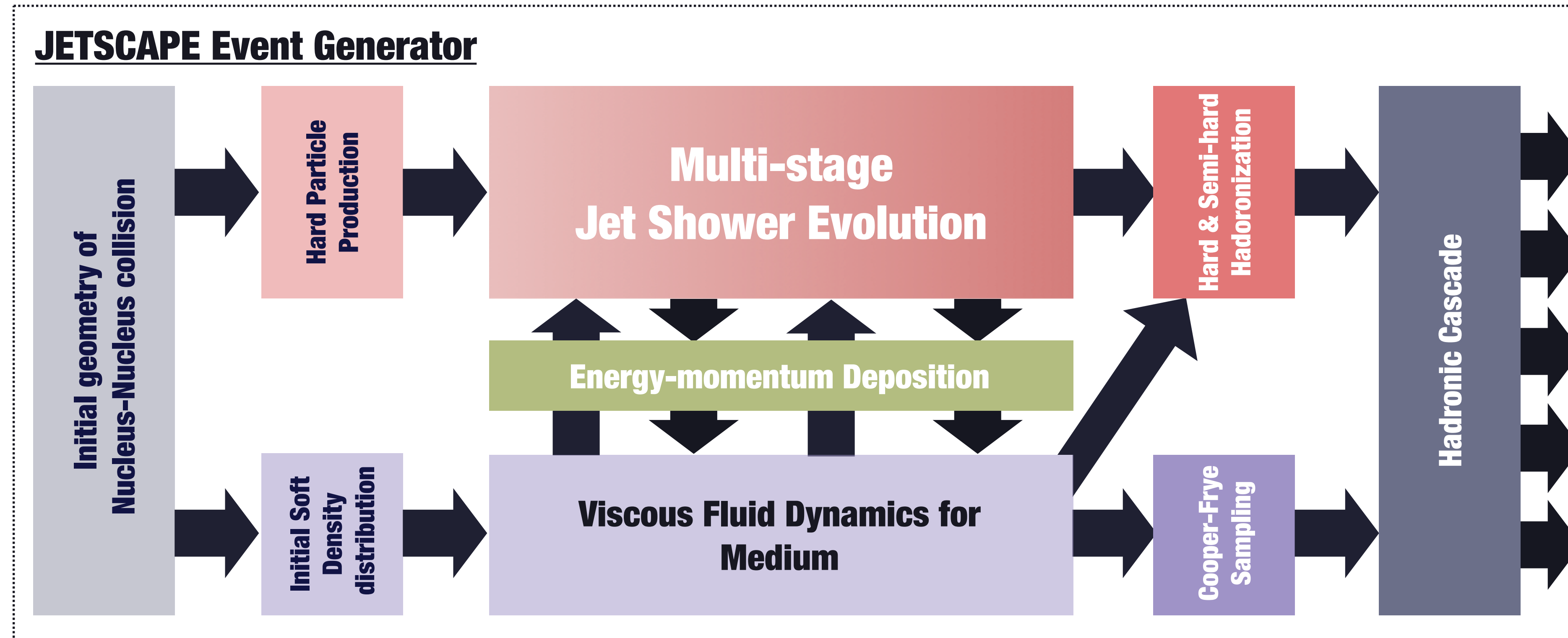
QCD相転移やQGP生成のモデル化による
重イオン衝突の時空発展の理解に向けた理論・実験共同研究会

September 24th, 2021

Jet Evolution in JETSCAPE

JETSCAPE framework

- **MC event generator package for heavy ion collisions**
 - General, modular and extensible
 - Communication between modules

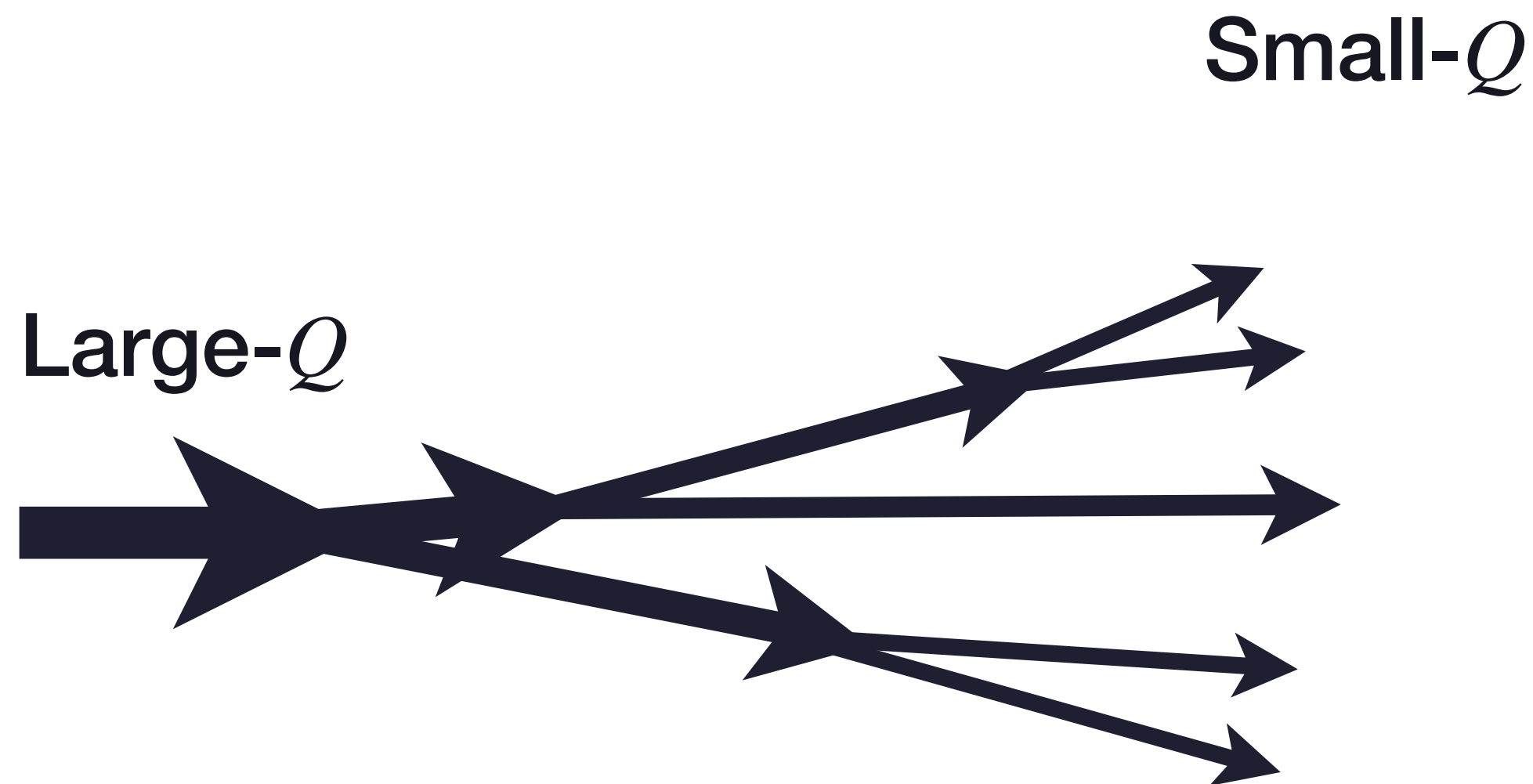


Multi-scale jet evolution

Majumder, Putschke (16), JETSCAPE (17)

In-vacuum

- In-vacuum: Virtuality ordered splitting



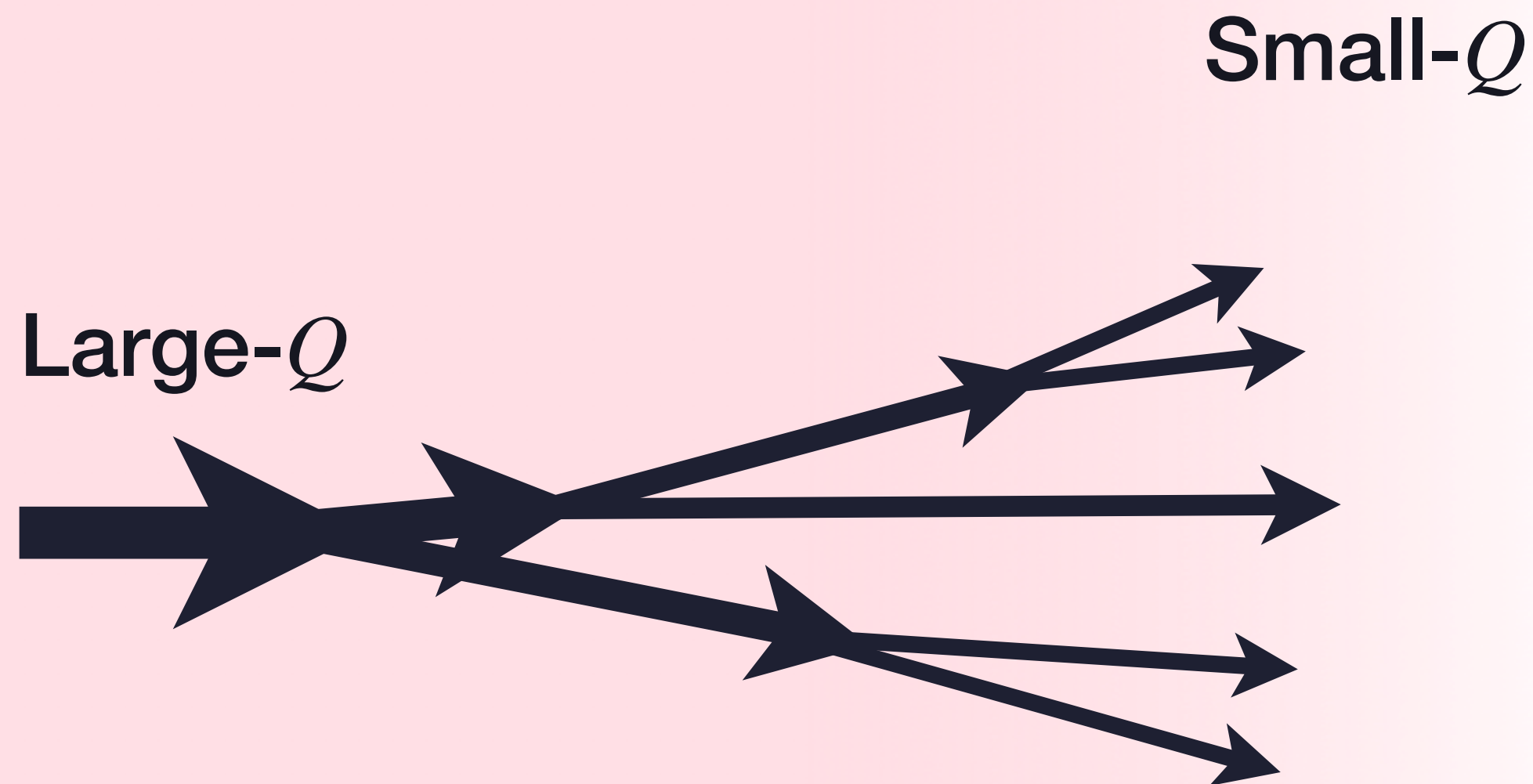
Q^2 : virtuality (off-shellness)

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In-medium

- In-vacuum: Virtuality ordered splitting

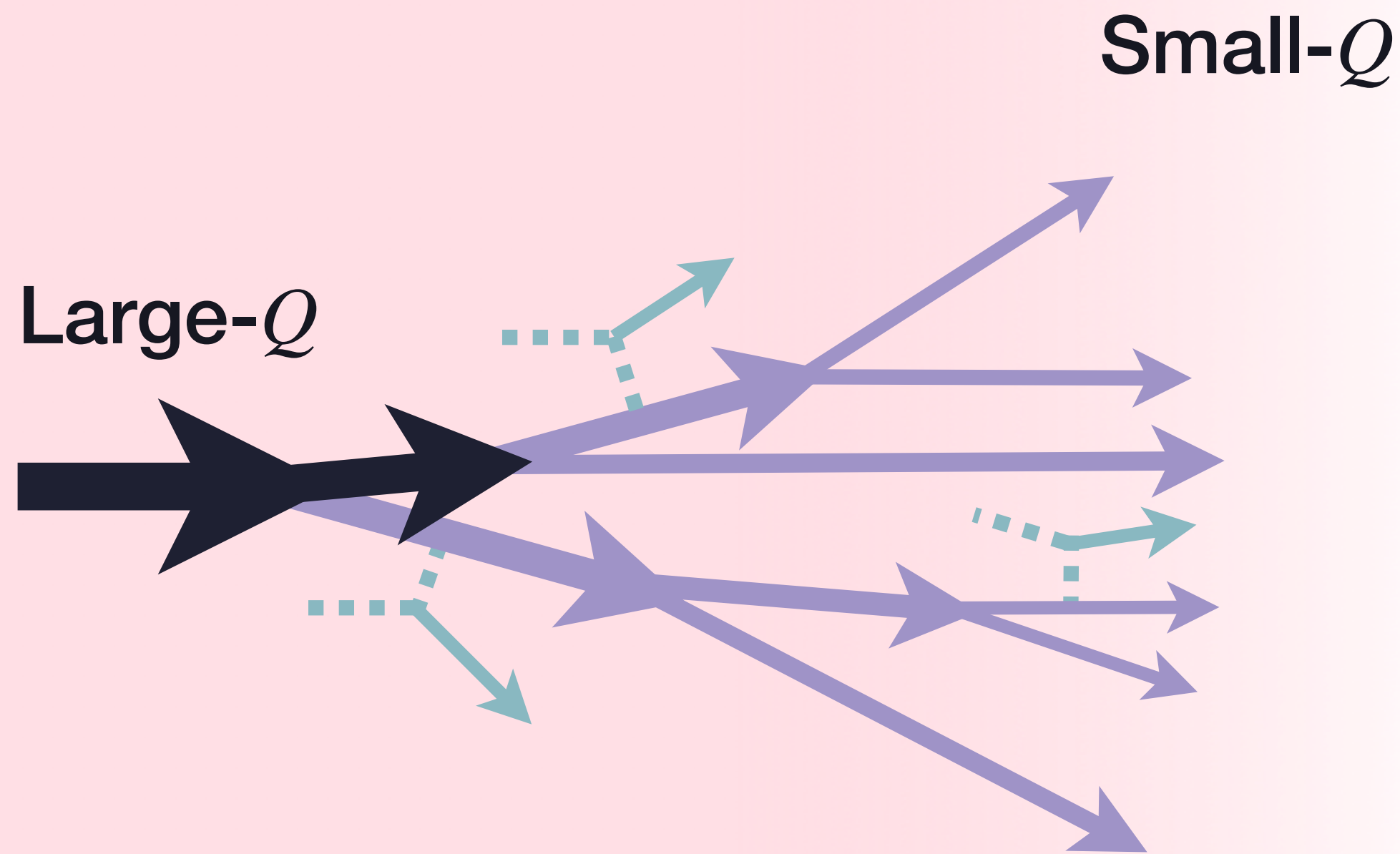


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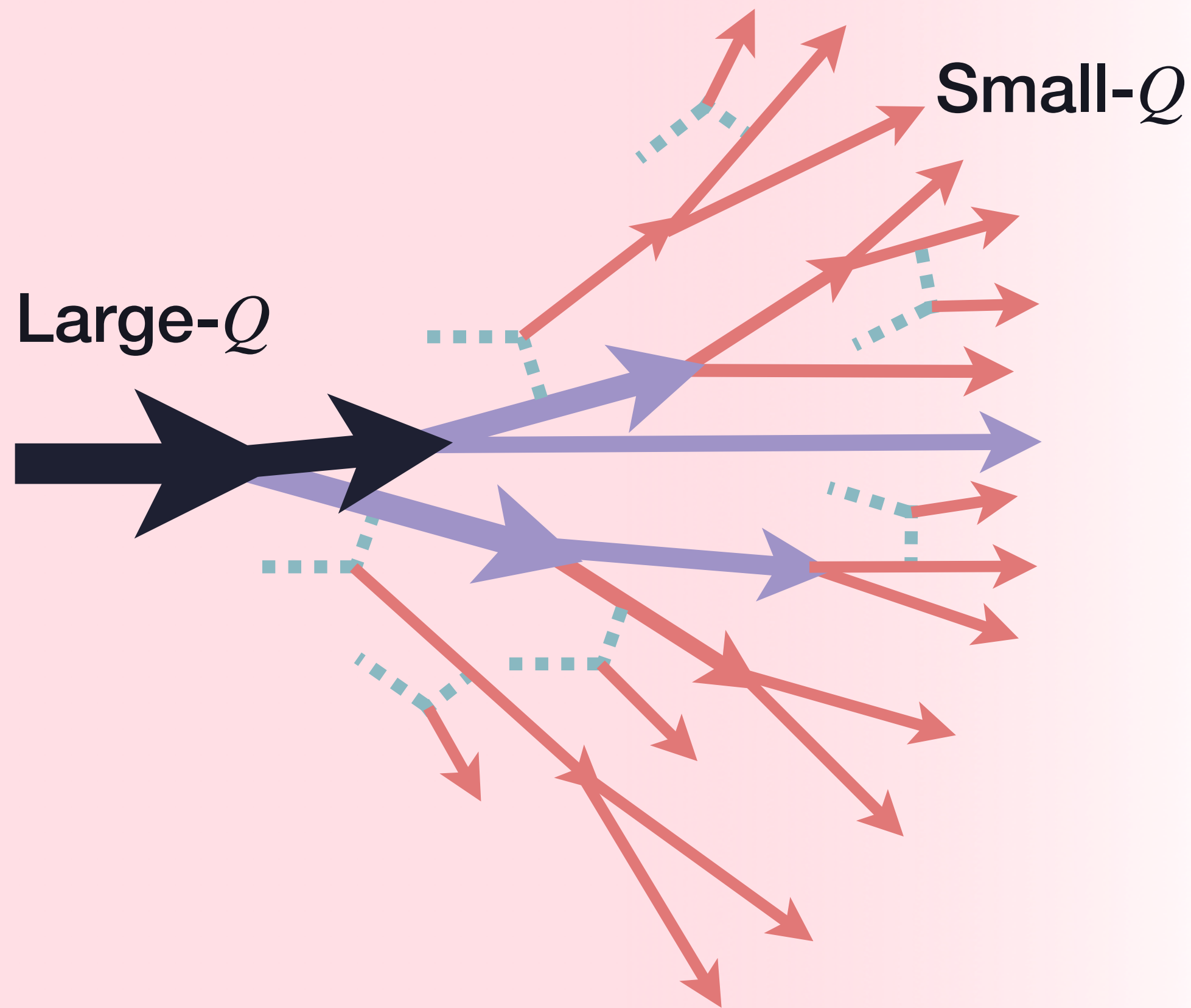
- In-vacuum: Virtuality ordered splitting
- Large- Q : Medium effect on the top of in-vacuum splitting
(Medium modified splitting)

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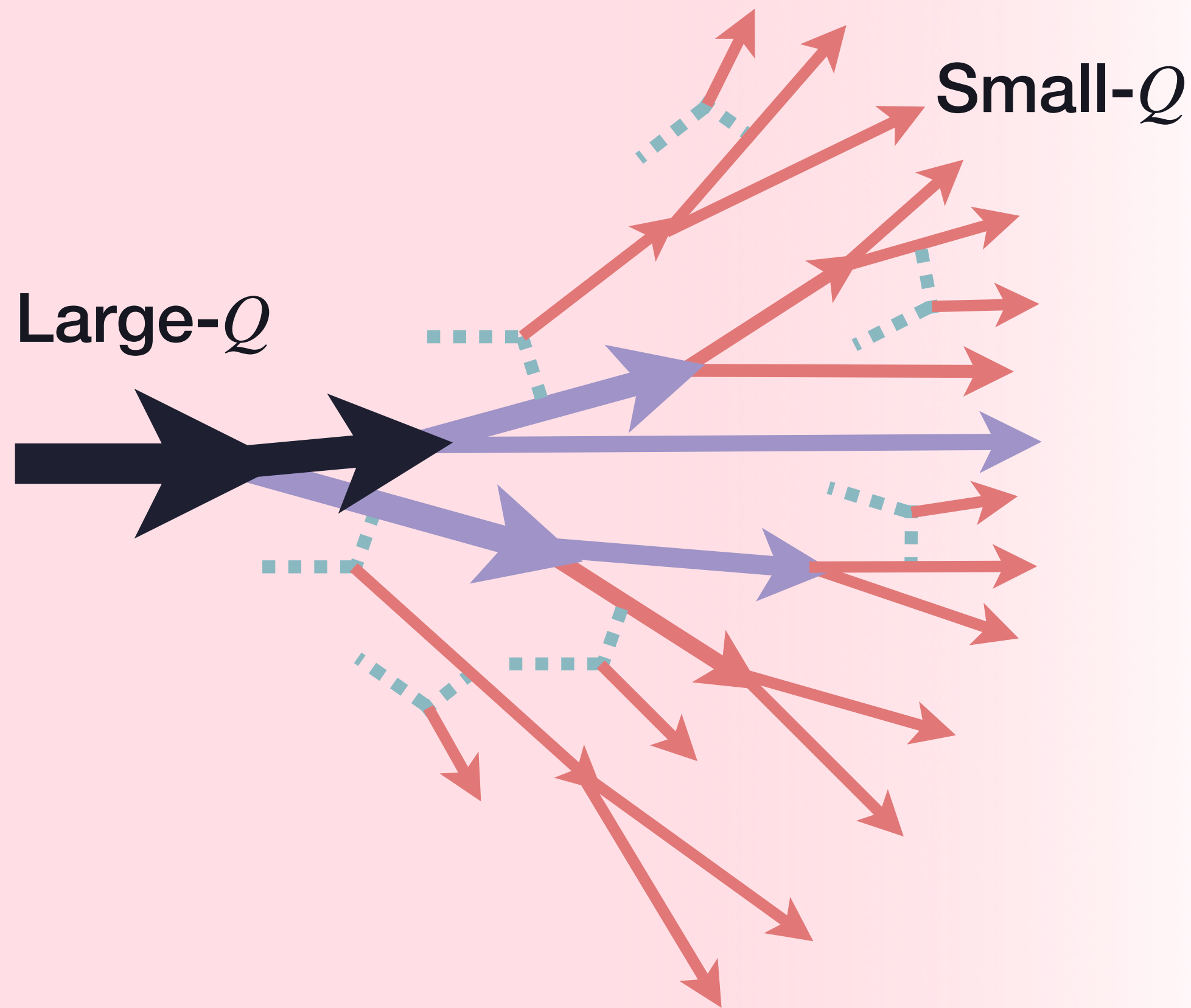
- In-vacuum: Virtuality ordered splitting
- Large- Q : Medium effect on the top of in-vacuum splitting
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- Small- Q : Splitting driven almost purely by medium effect
(Medium induced splitting)

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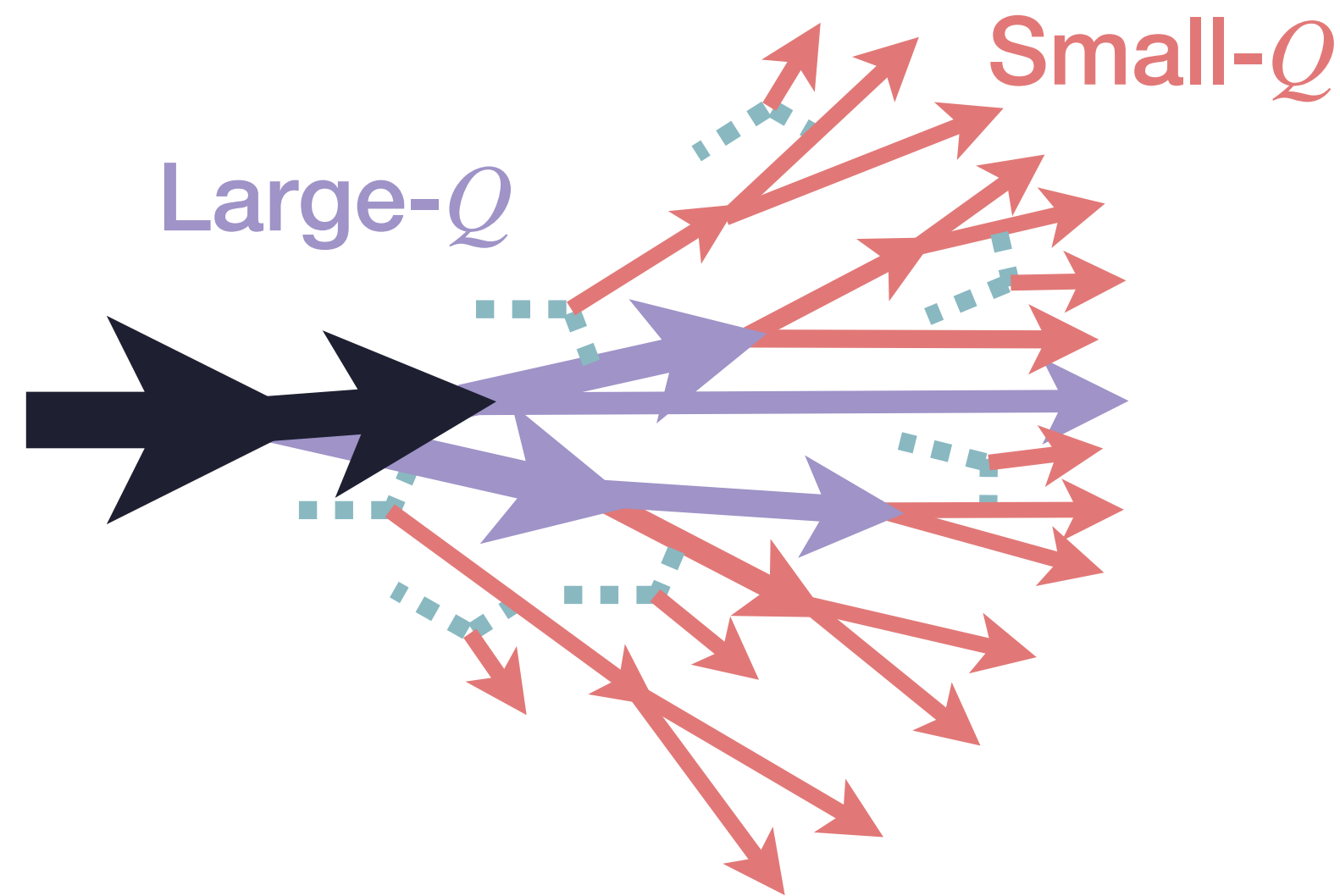
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- Large- Q : Medium effect on the top of in-vacuum splitting
(Medium modified splitting)
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Cannot be described by a single model
→ Combination of multiple models

Q^2 : virtuality (off-shellness)

Multi-stage description for jet evolution

JETSCAPE (17)

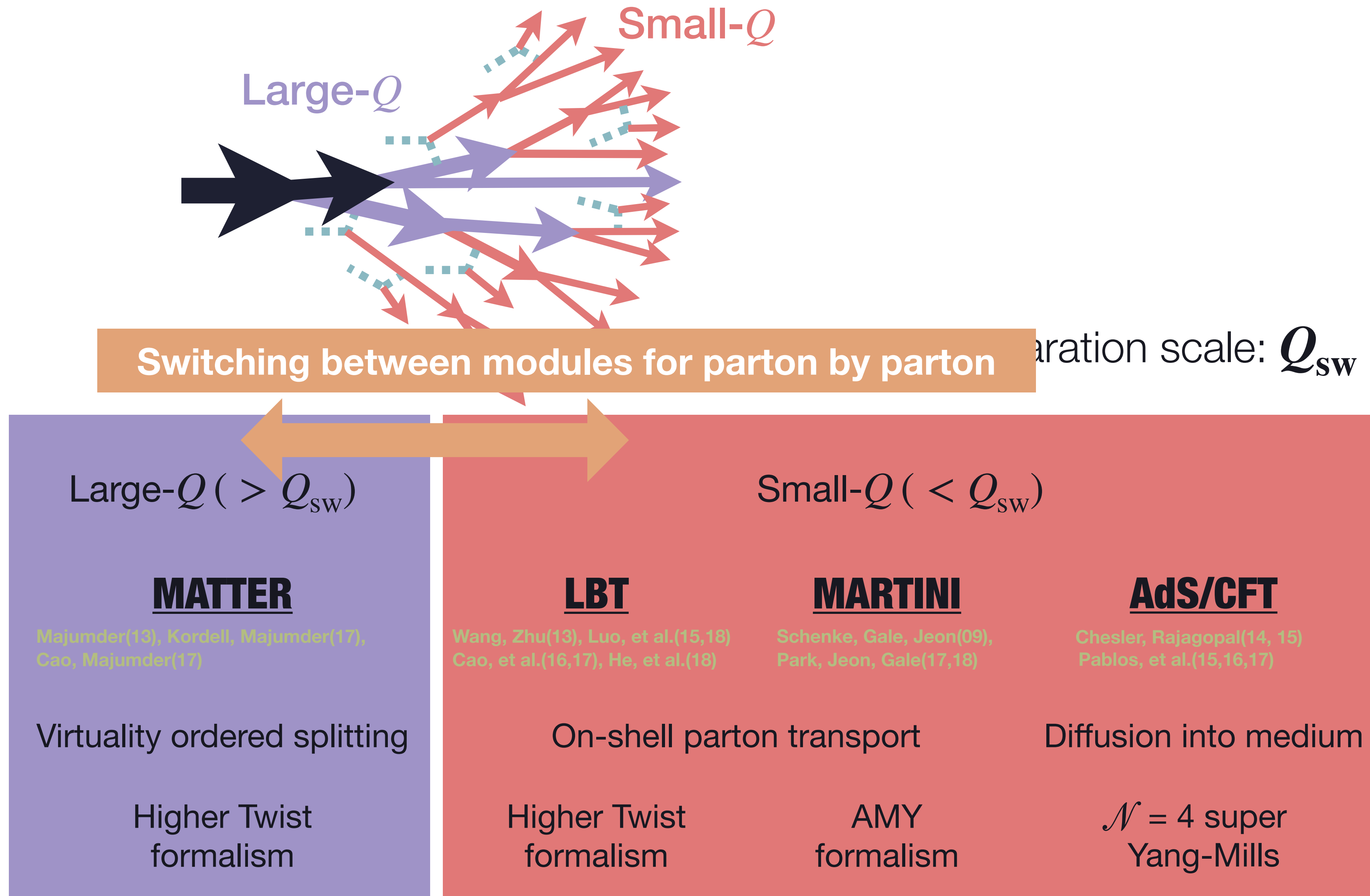


Virtuality separation scale: Q_{sw}

Large- Q ($> Q_{sw}$)	Small- Q ($< Q_{sw}$)		
<u>MATTER</u>	<u>LBT</u>	<u>MARTINI</u>	<u>AdS/CFT</u>
Majumder(13), Kordell, Majumder(17), Cao, Majumder(17)	Wang, Zhu(13), Luo, et al.(15,18) Cao, et al.(16,17), He, et al.(18)	Schenke, Gale, Jeon(09), Park, Jeon, Gale(17,18)	Chesler, Rajagopal(14, 15) Pablos, et al.(15,16,17)
Virtuality ordered splitting	On-shell parton transport	Diffusion into medium	
Higher Twist formalism	Higher Twist formalism	AMY formalism	$\mathcal{N} = 4$ super Yang-Mills

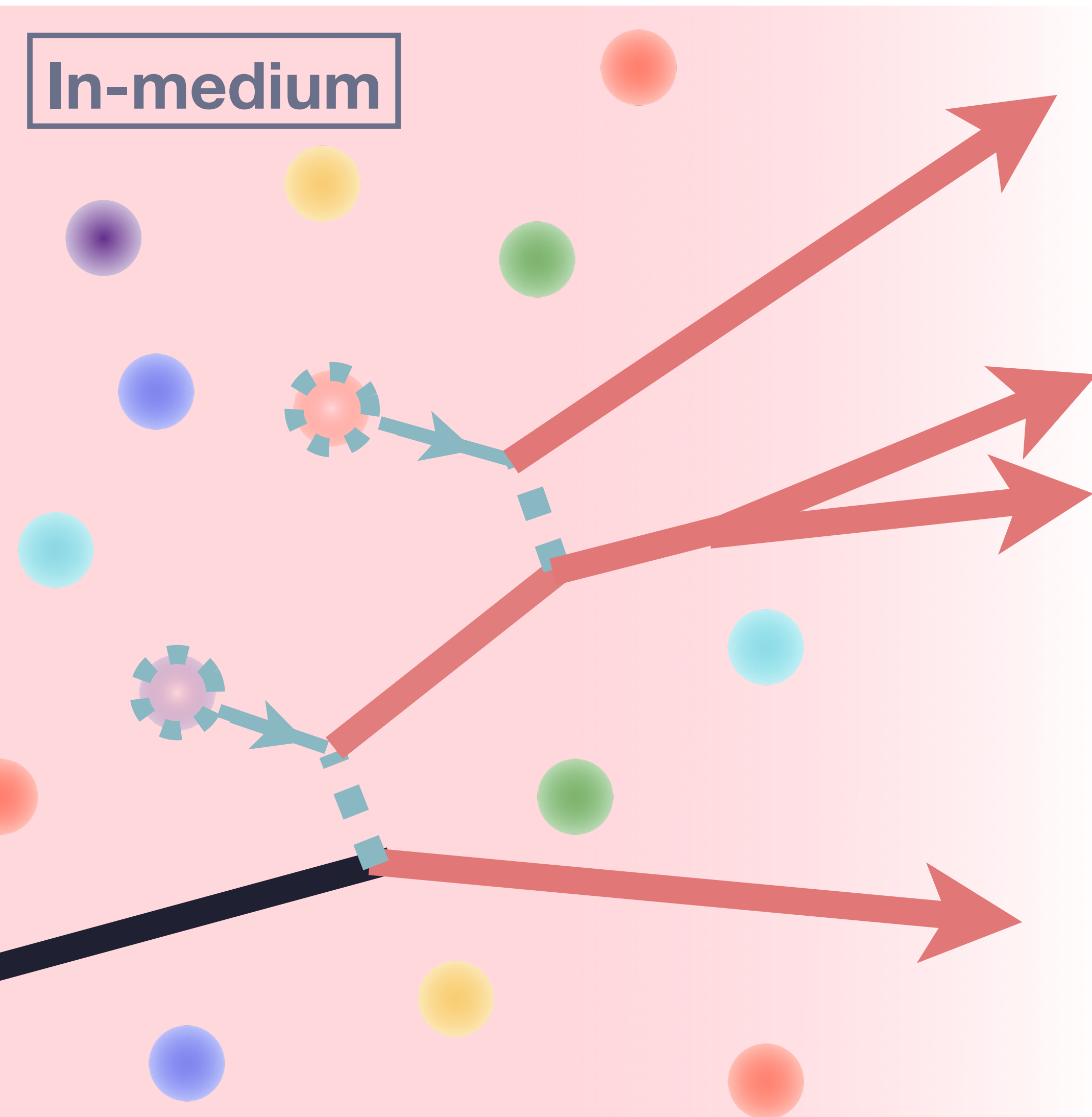
Multi-stage description for jet evolution

JETSCAPE (17)



Medium response by weakly-coupled recoils

Zapp *et al.* ('13), Wang, Zhu (13), Luo, *et al.* (15,18), Park, Jeon, Gale (18), Cao, Majumder (18)



● Recoils

- Medium partons kicked out by jet partons
- Evolve as small- Q^2 partons in jet shower
- Infinite thermalization time ($E > E_{\text{med}}$)

● Hole: Picked up energy and momentum

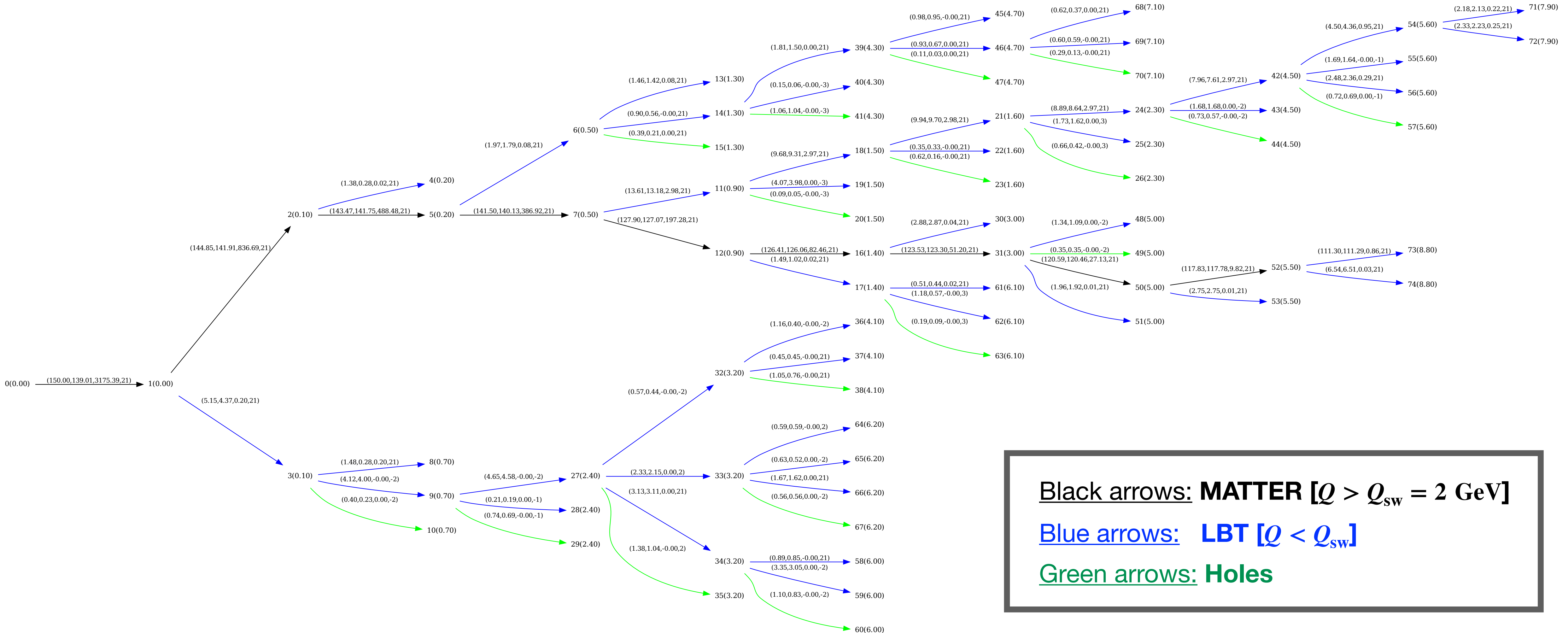
- Sampled from thermal medium
- Subtracted from final signal

$$\left. \frac{dp^\mu}{d\eta d\phi} \right|_{\text{signal}} = \left. \frac{dp^\mu}{d\eta d\phi} \right|_{\text{jet shower}} - \left. \frac{dp^\mu}{d\eta d\phi} \right|_{\text{picked-up}}$$

Multi-stage description for jet evolution

JETSCAPE (17)

Graph of parton shower generated by JETSCAPE

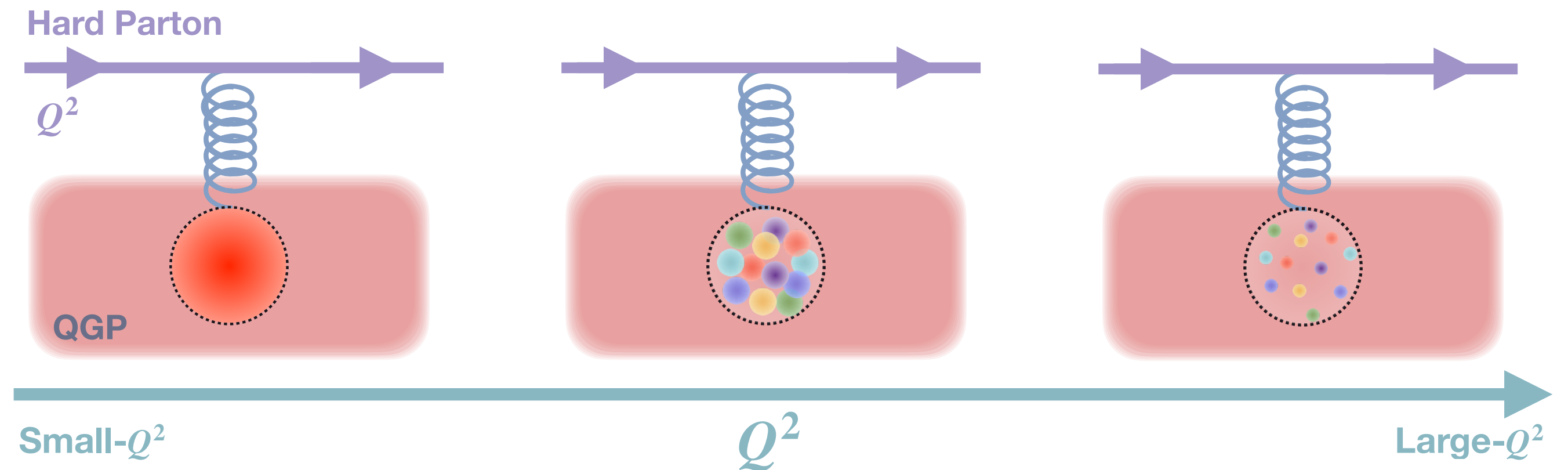
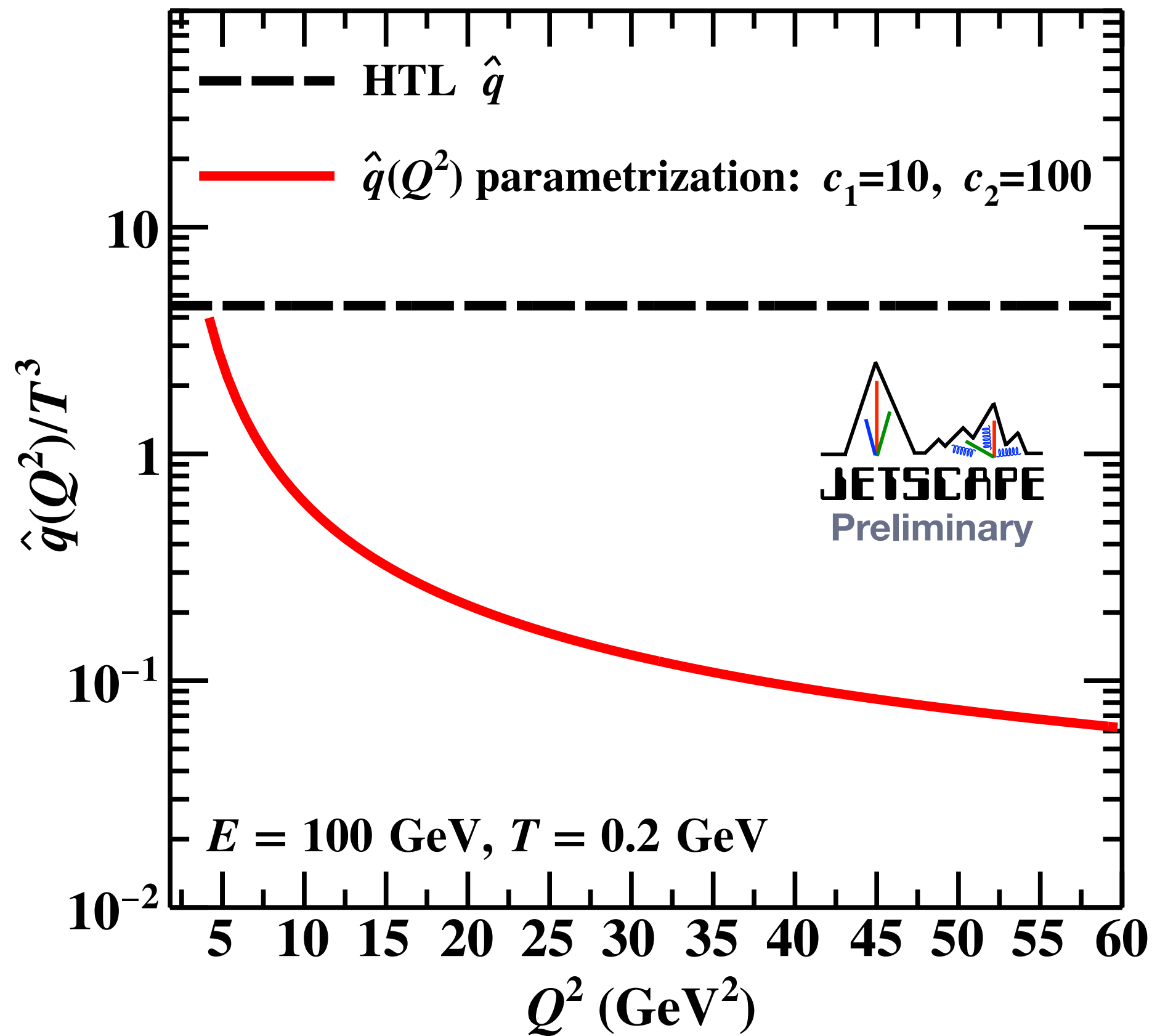


Recent Update

JERSCAPE (in preparation)

- **Virtuality dependence in jet quenching parameter \hat{q}**

- Based on scale evolution of QGP constituent distribution
Kumar, Majumder, Shen (20)

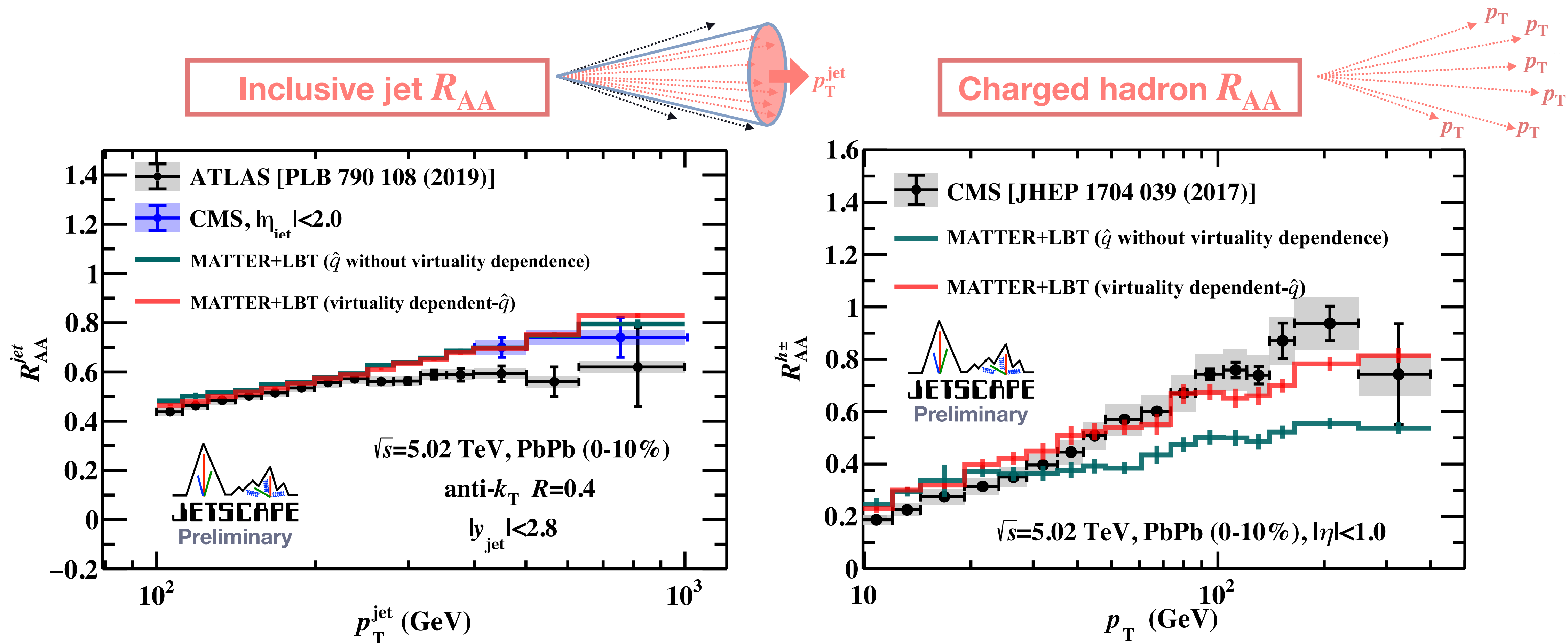


- Less interaction for larger virtuality partons
- Extend the model applicability to further broader scale

Jet and high- p_T particle energy loss

JERSCAPE (in preparation)

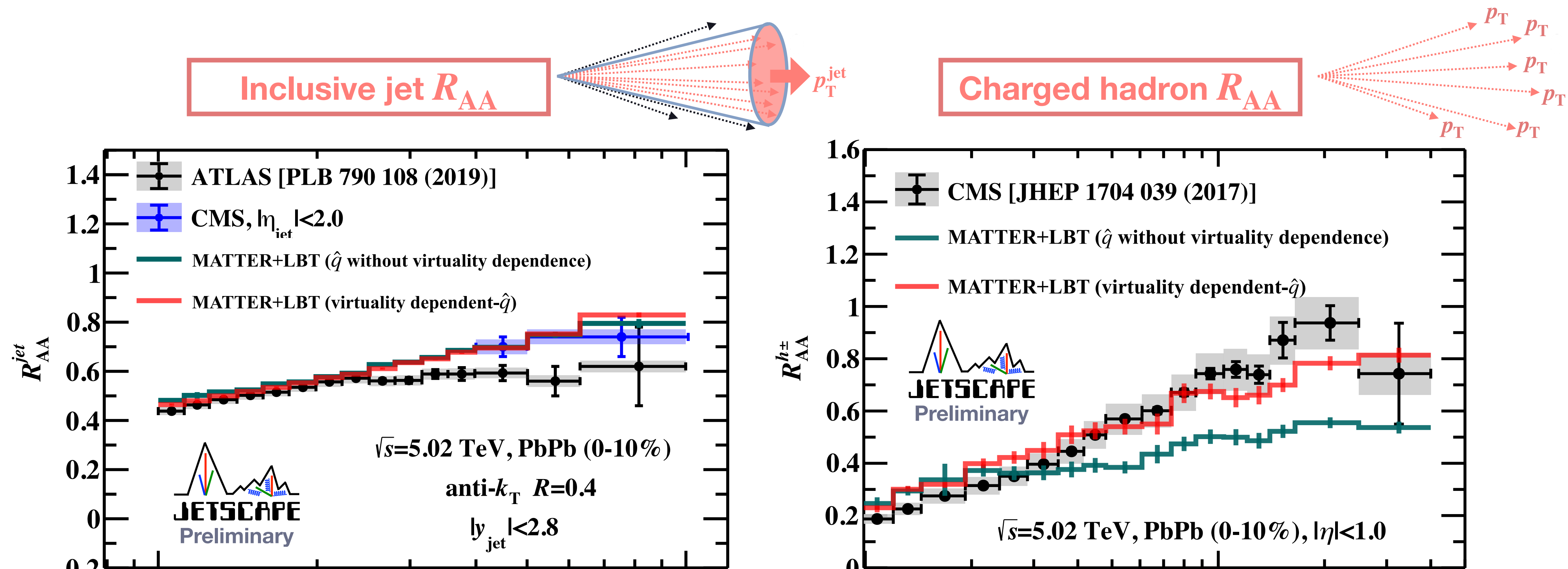
- Jet and high- p_T particle energy loss for PbPb@5.02 TeV



Jet and high- p_T particle energy loss

JERSCAPE (in preparation)

- Jet and high- p_T particle energy loss for PbPb@5.02 TeV



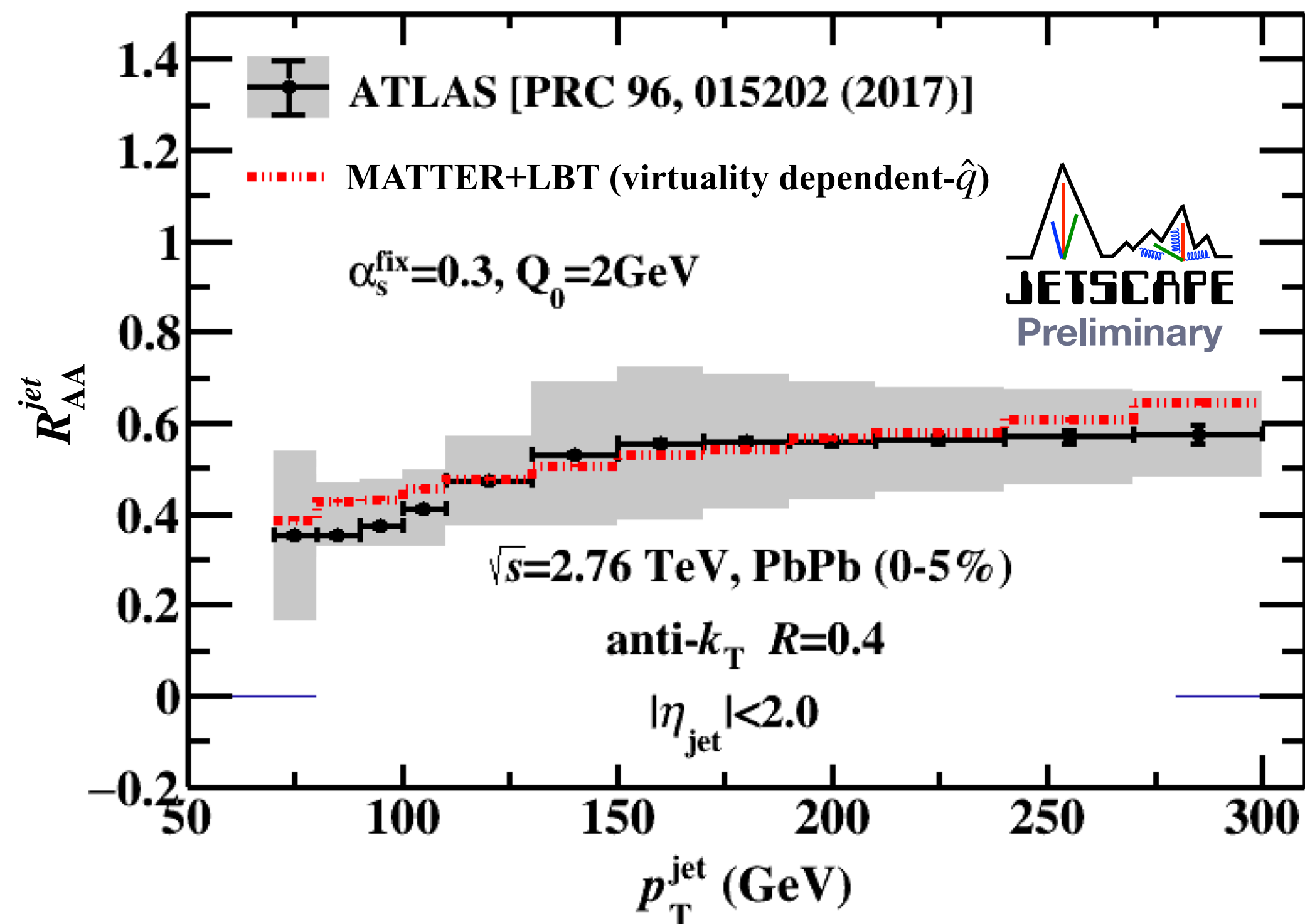
- Very first success in simultaneous description of data for jet and hadrons
- Significant effect of virtuality dependence in energy loss

Jet and high- p_T particle energy loss

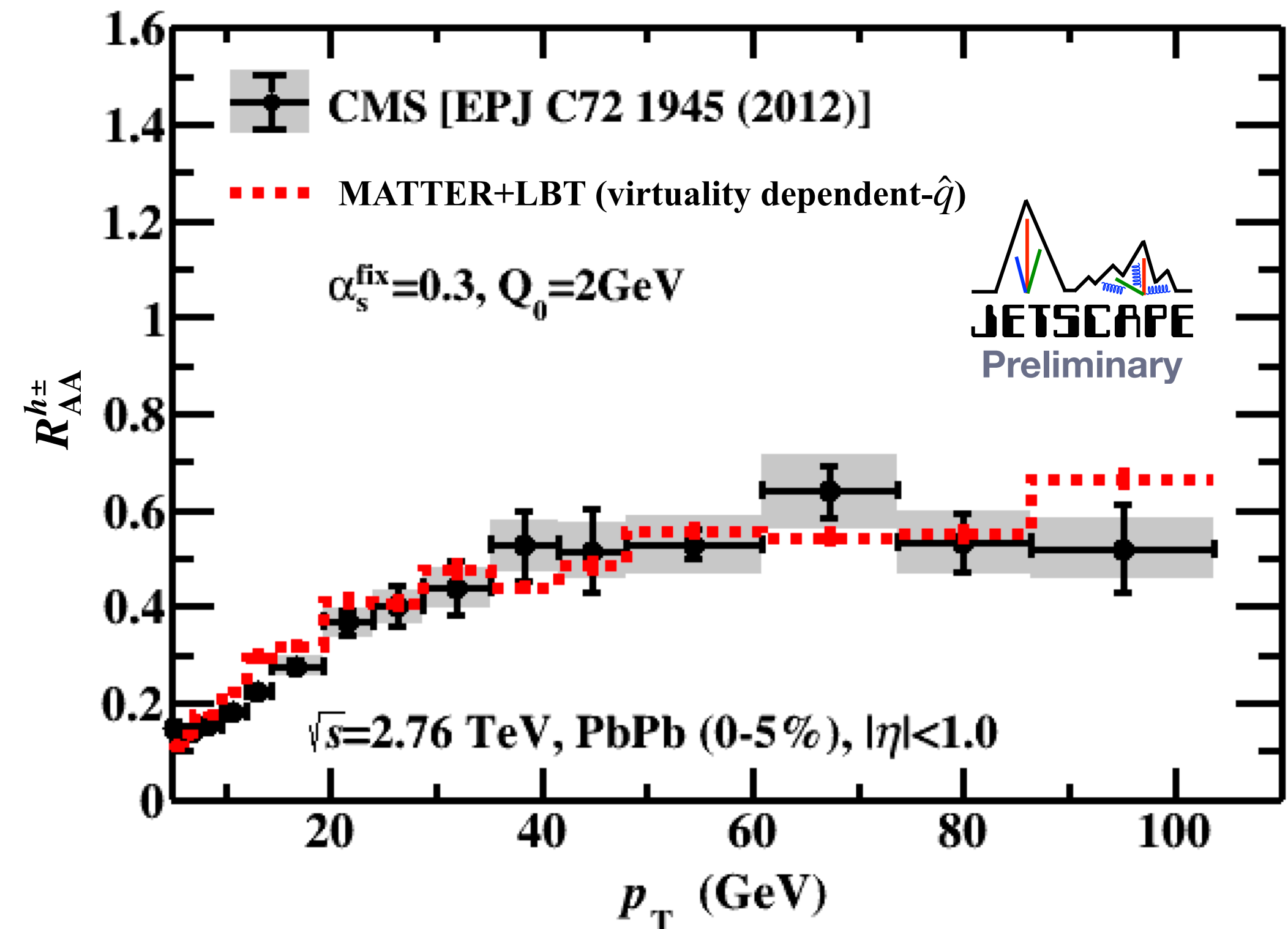
- Jet and high- p_T particle energy loss for PbPb@2.76 TeV

The same parameter set as 5.02 TeV is used

Inclusive jet R_{AA}



Charged hadron R_{AA}



Jet and high- p_T particle energy loss

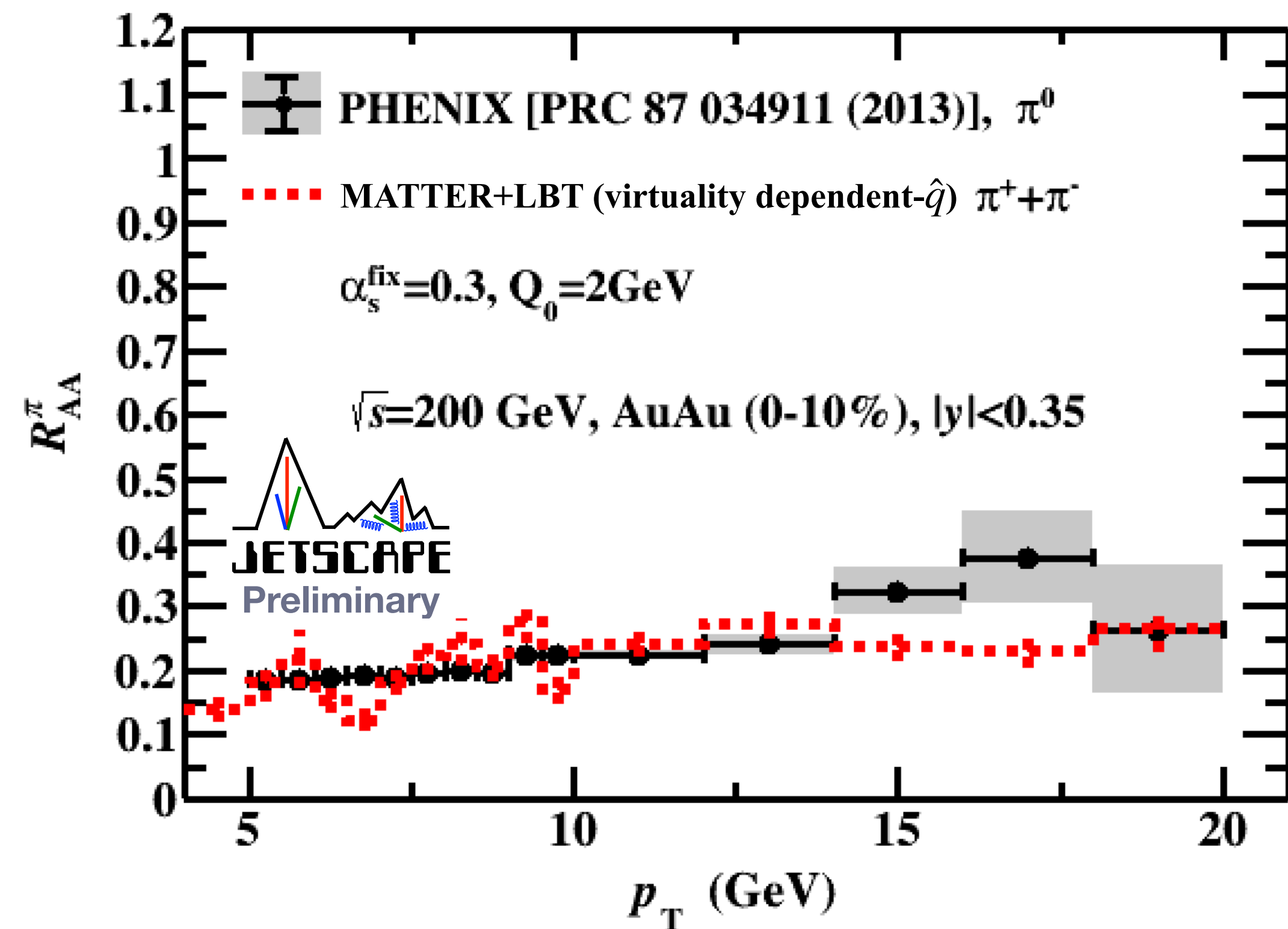
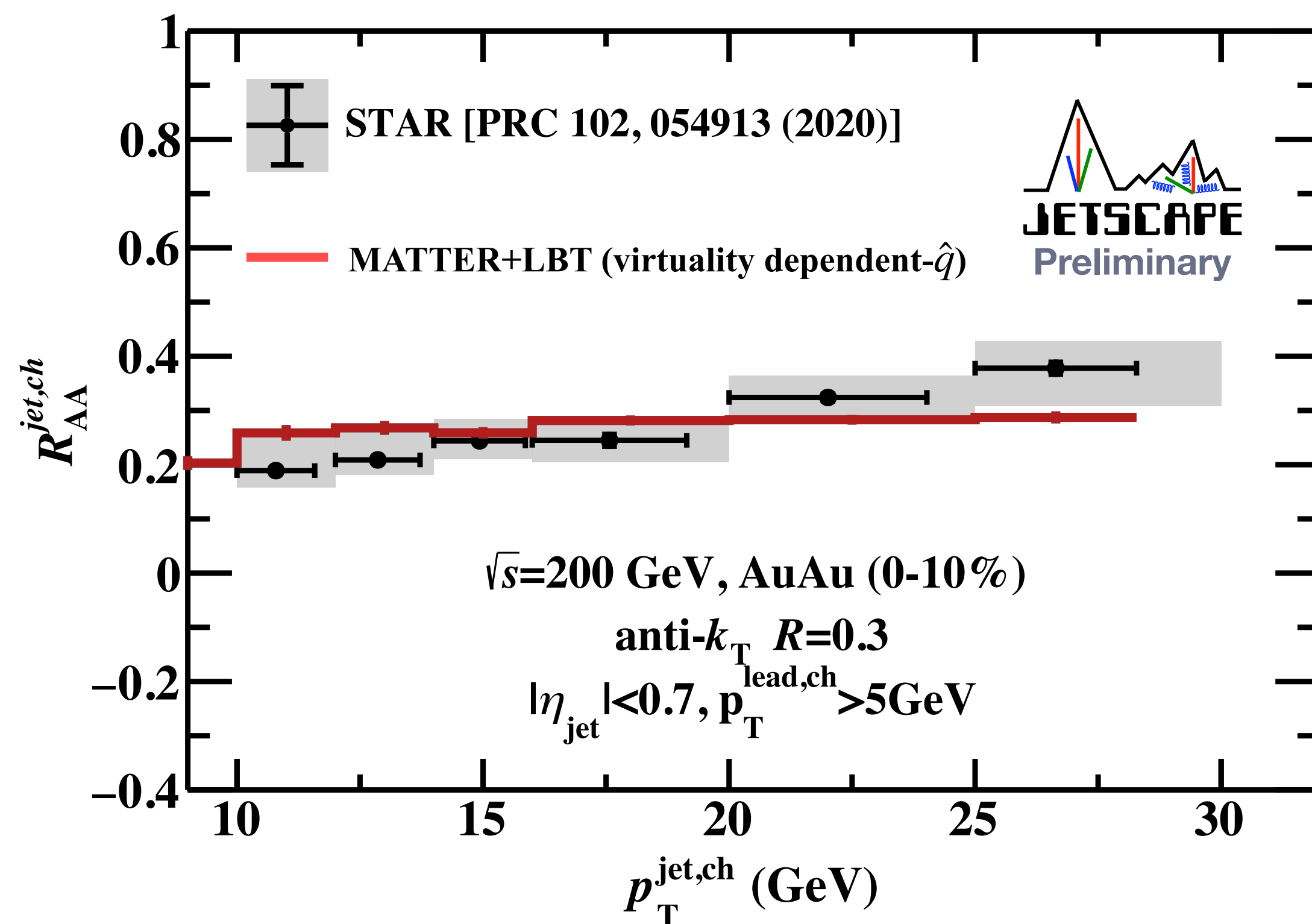
JERSCAPE (in preparation)

- Jet and high- p_T particle energy loss for AuAu@200 GeV

The same parameter set as 5.02 TeV is used

Charged jet R_{AA}

Pion R_{AA}



Jet and high- p_T particle energy loss

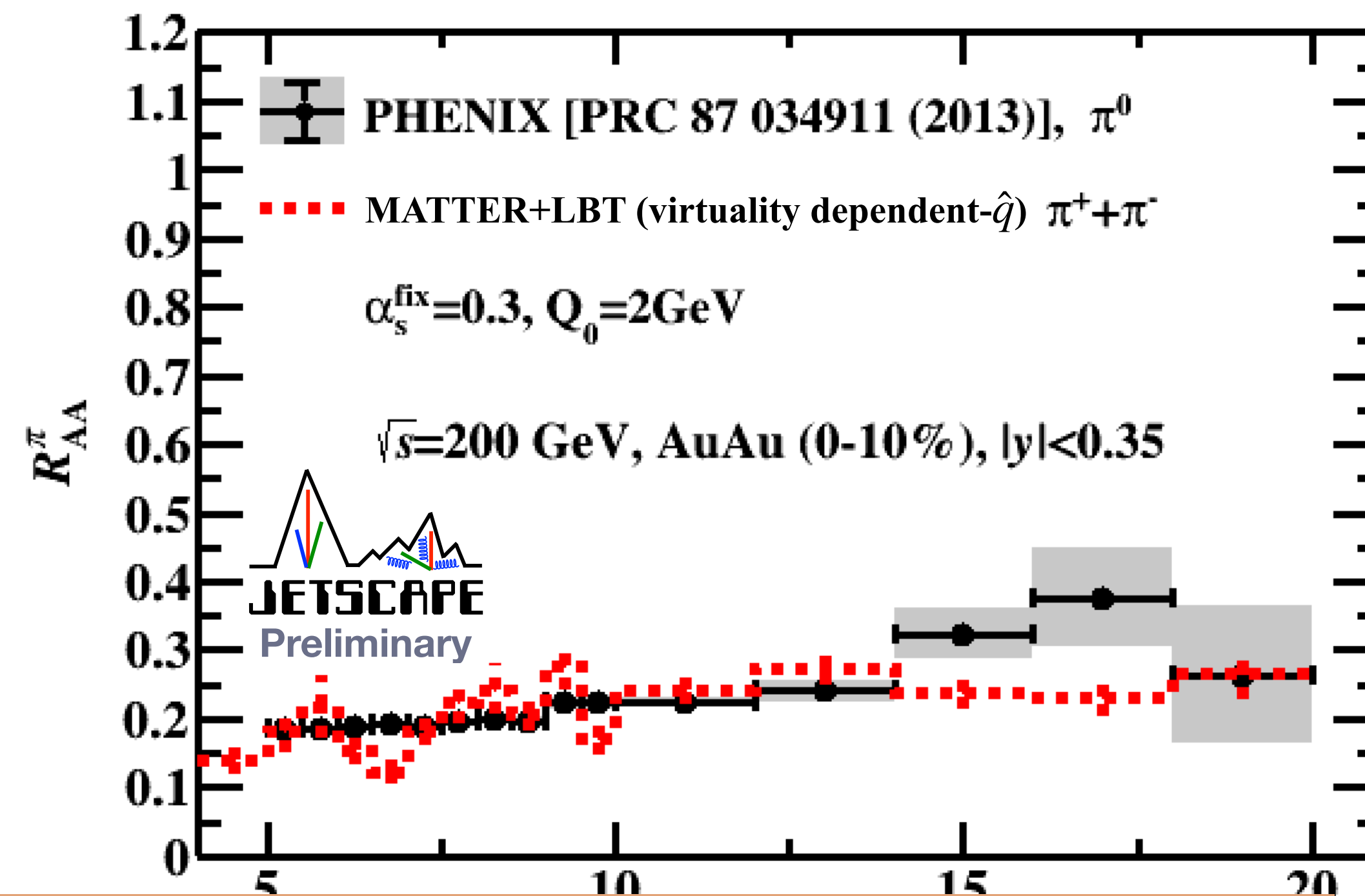
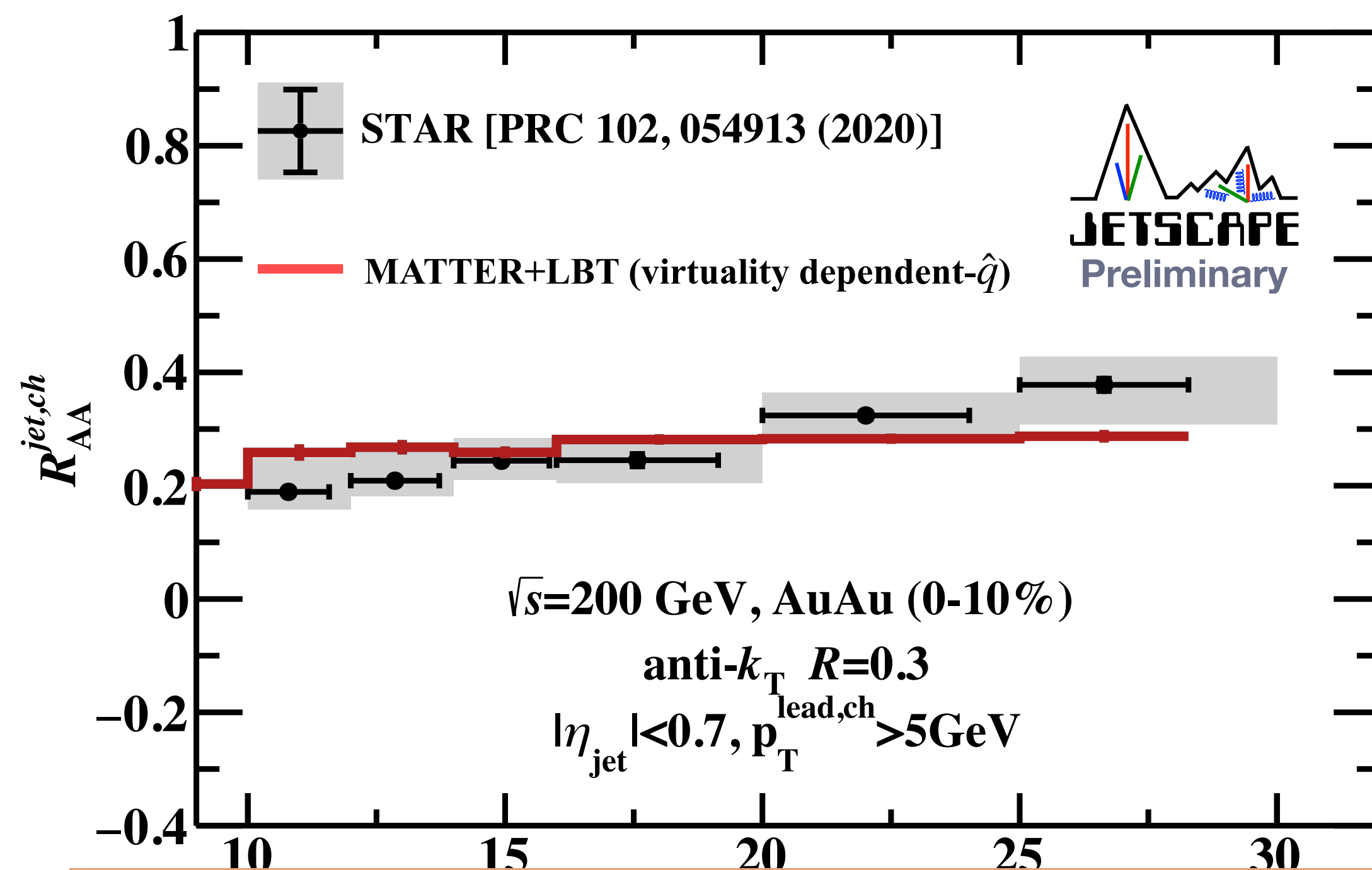
JERSCAPE (in preparation)

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Charged jet R_{AA}

Pion R_{AA}



Simultaneous description of different $\sqrt{s_{NN}}$ with the same parameter set

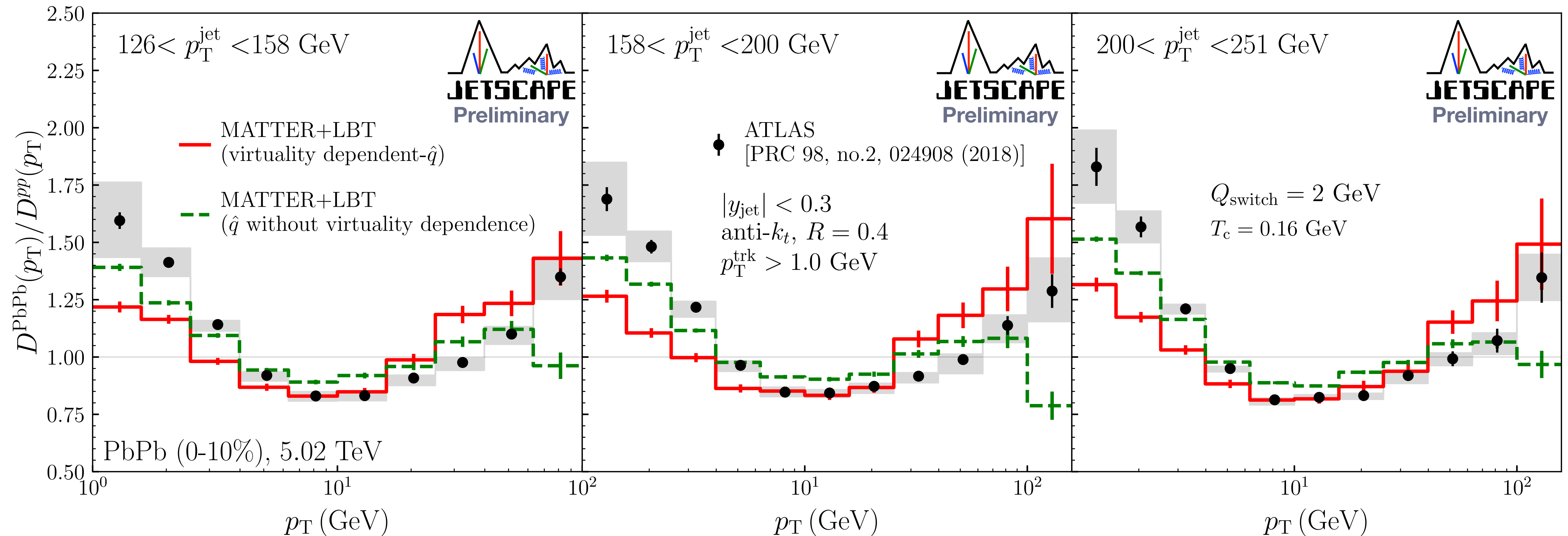
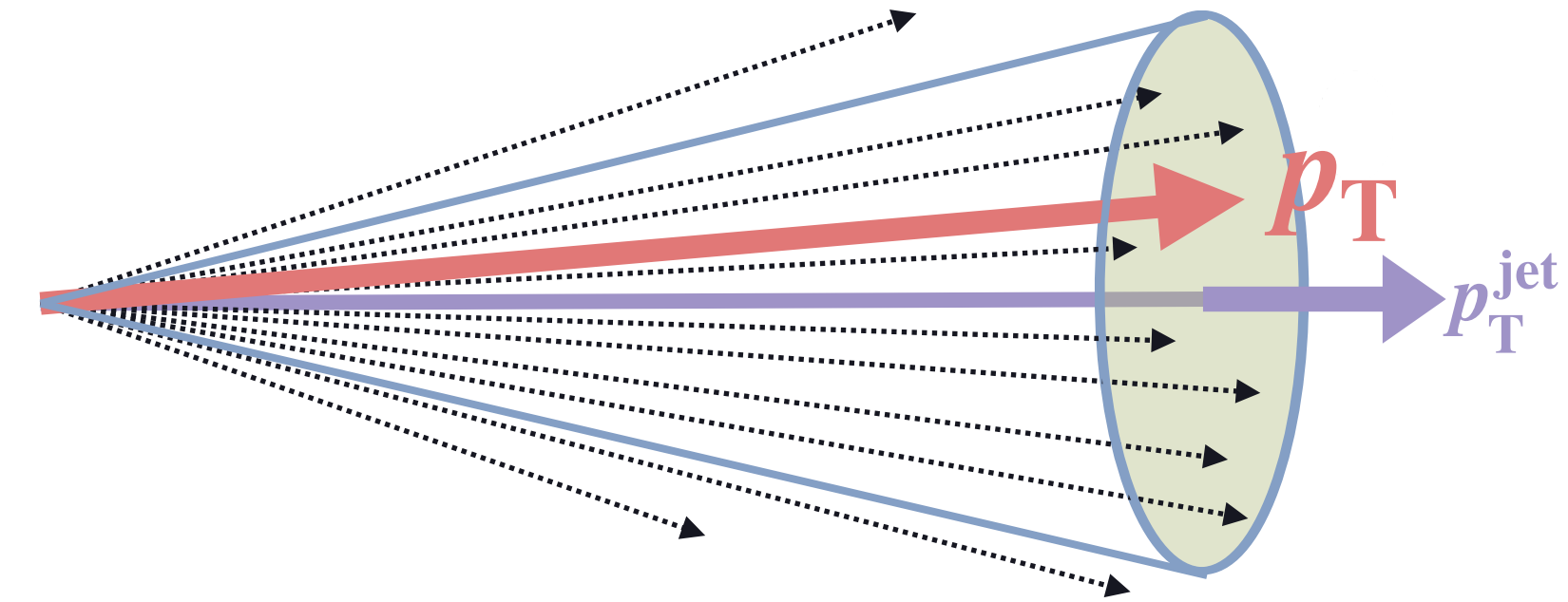
Jet substructure

JERSCAPE (in preparation)

● Jet Fragmentation Function

- p_T distribution of charged particle inside jets

$$D(p_T) = \frac{1}{N_{\text{jet}}} \sum_{\text{jet}} \left. \frac{dN_{\text{ch}}}{dp_T} \right|_{\text{in jet}}$$



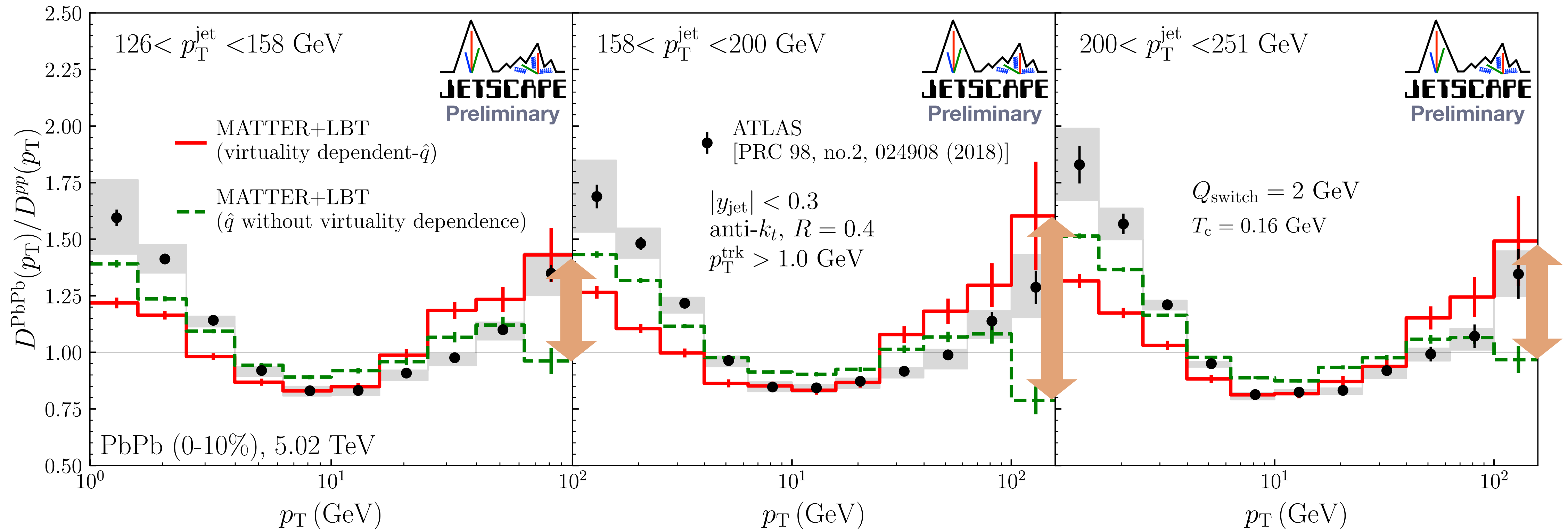
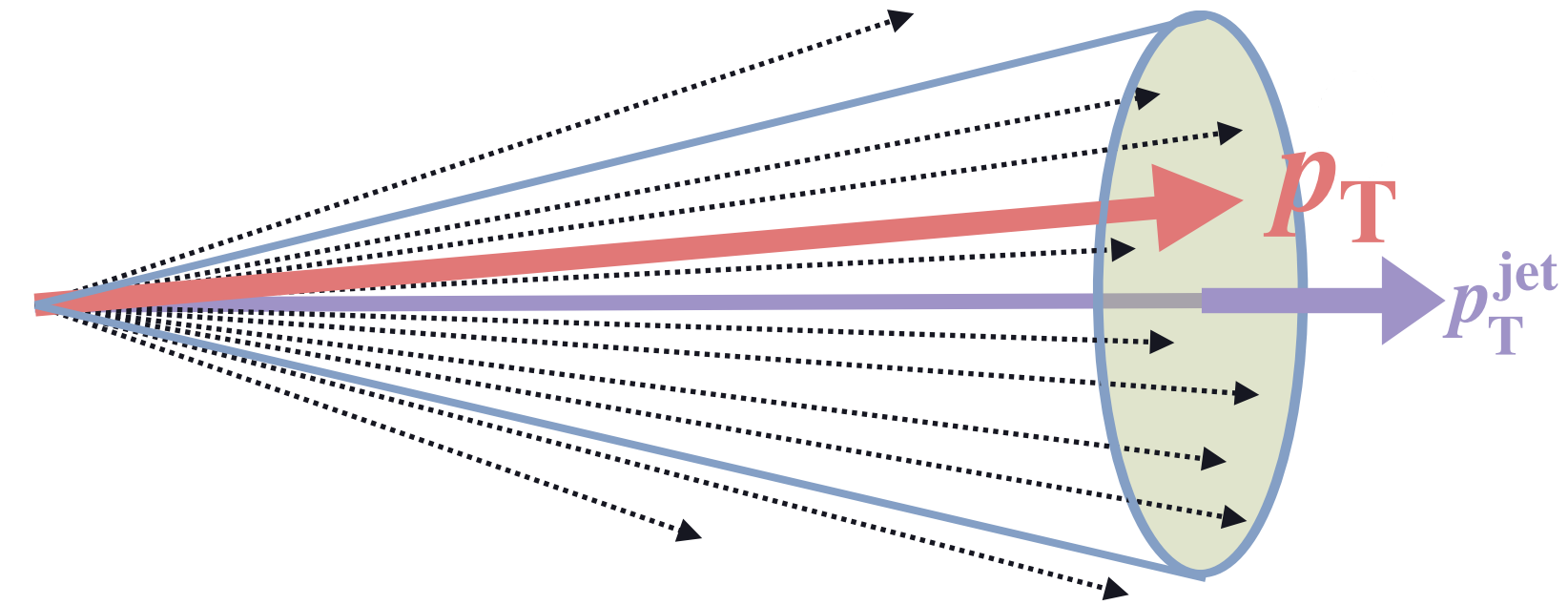
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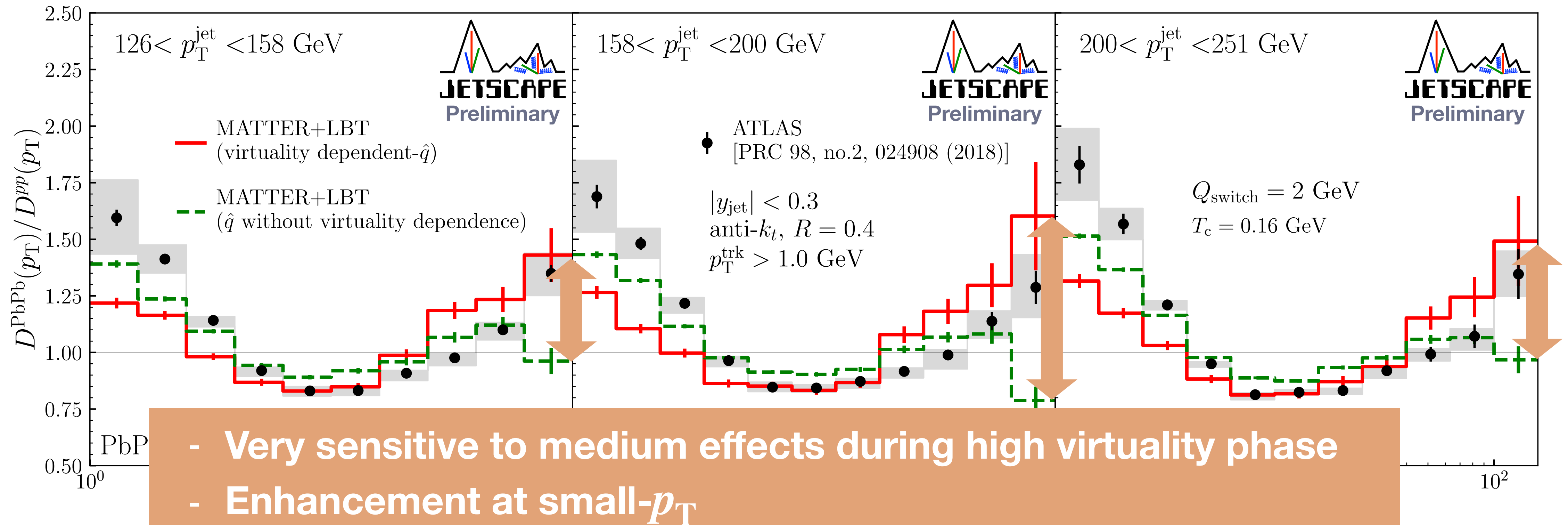
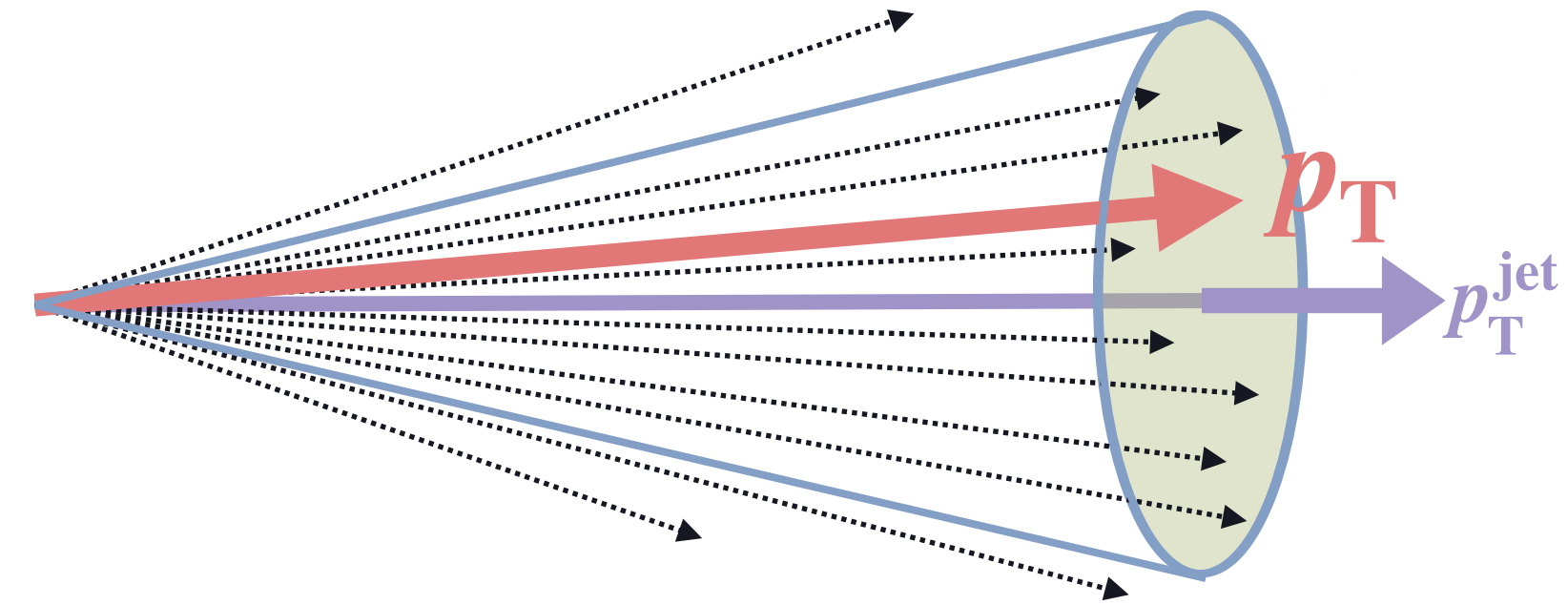
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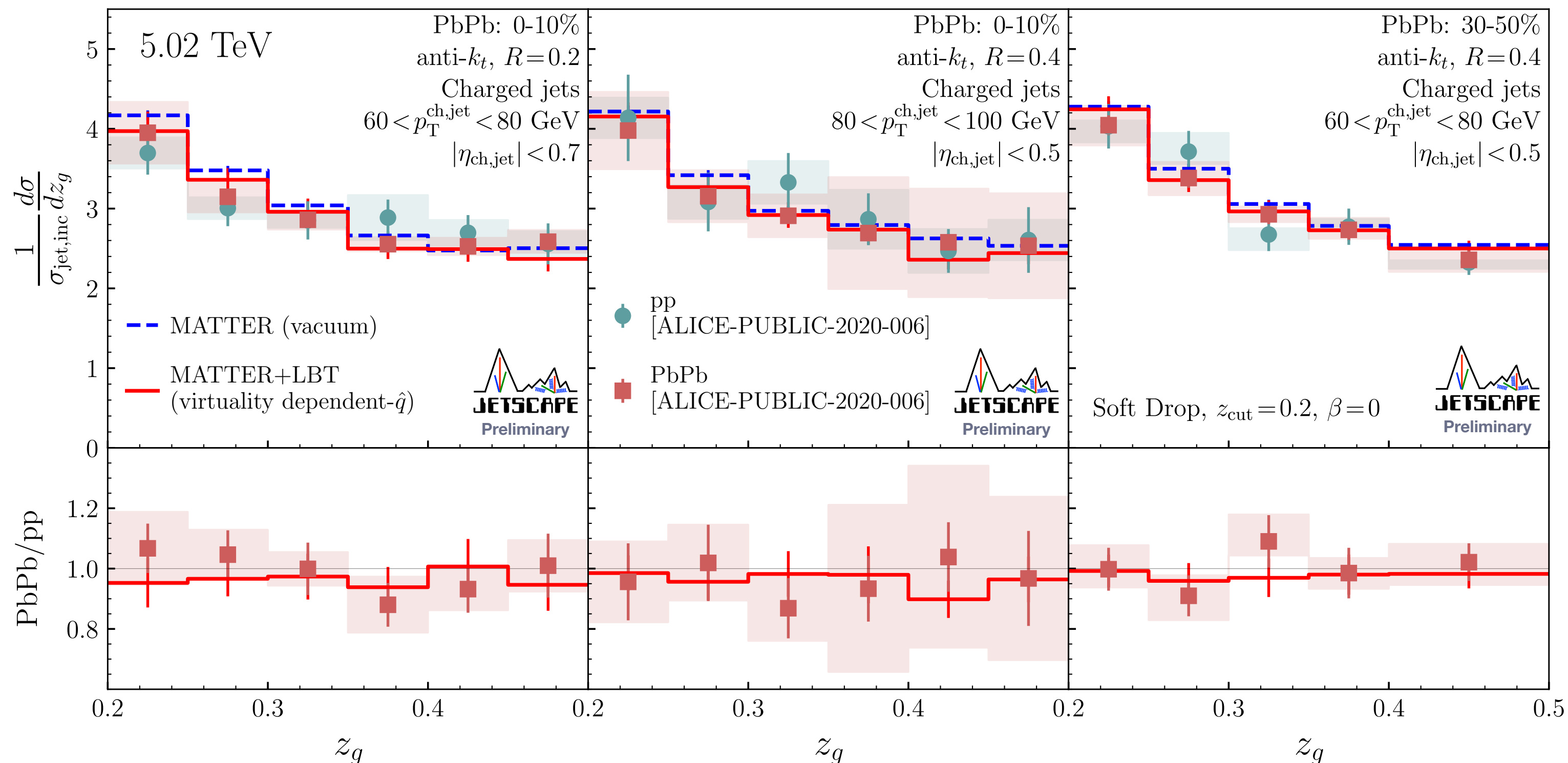
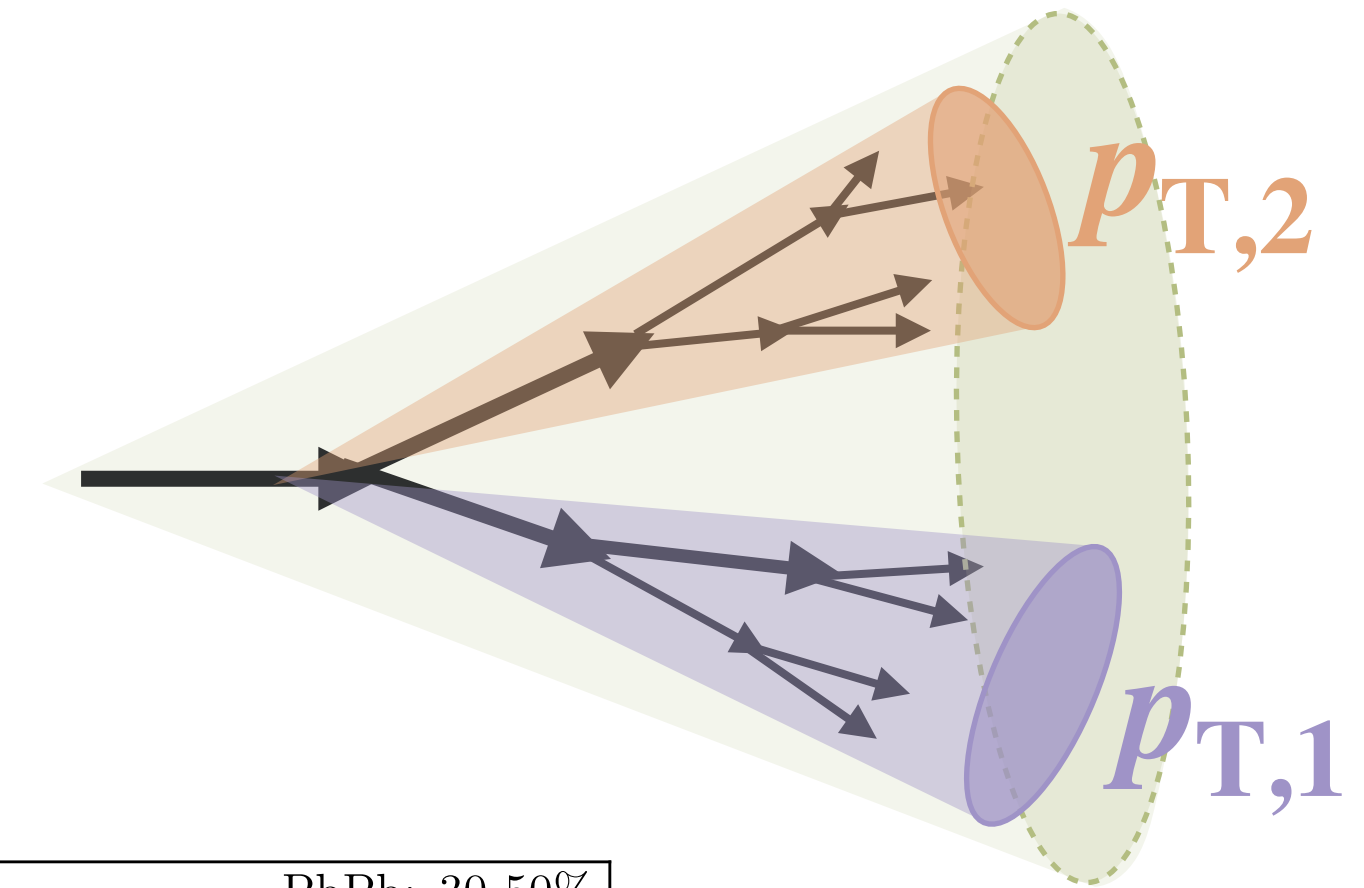
Jet substructure

JERSCAPE (in preparation)

● Jet splitting function

- Momentum fraction in the hardest splitting of jet (z_g)

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}}$$



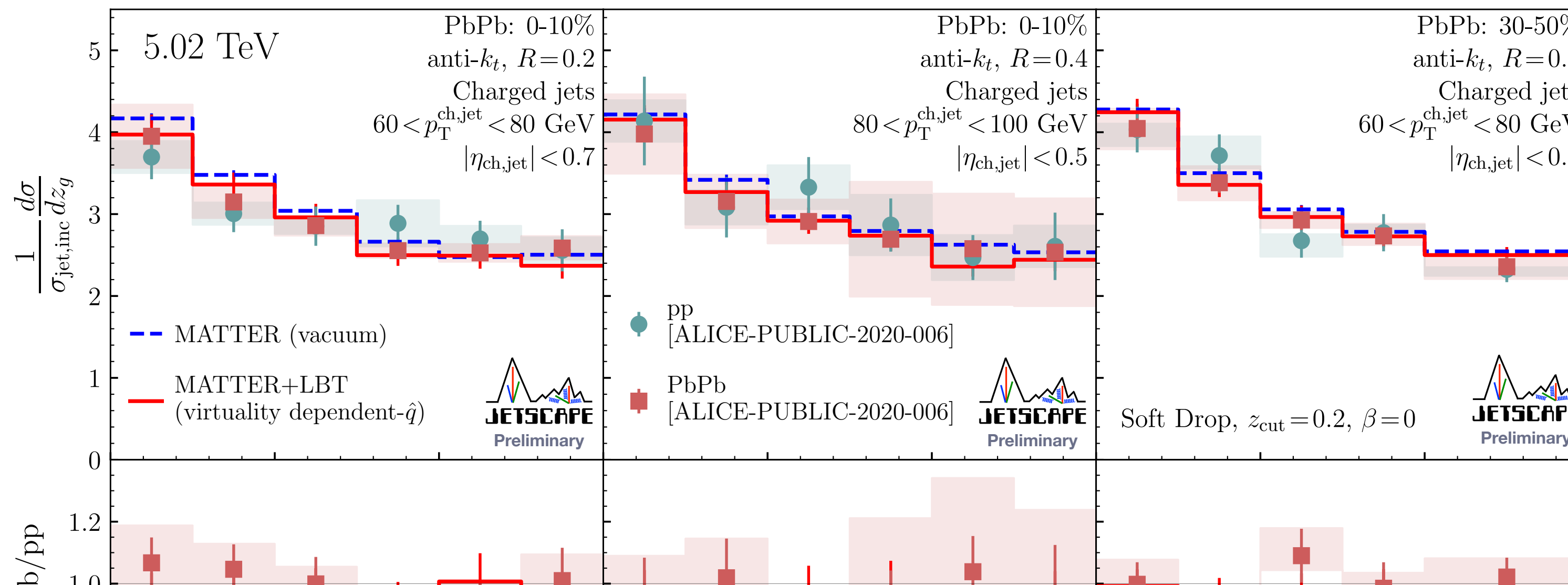
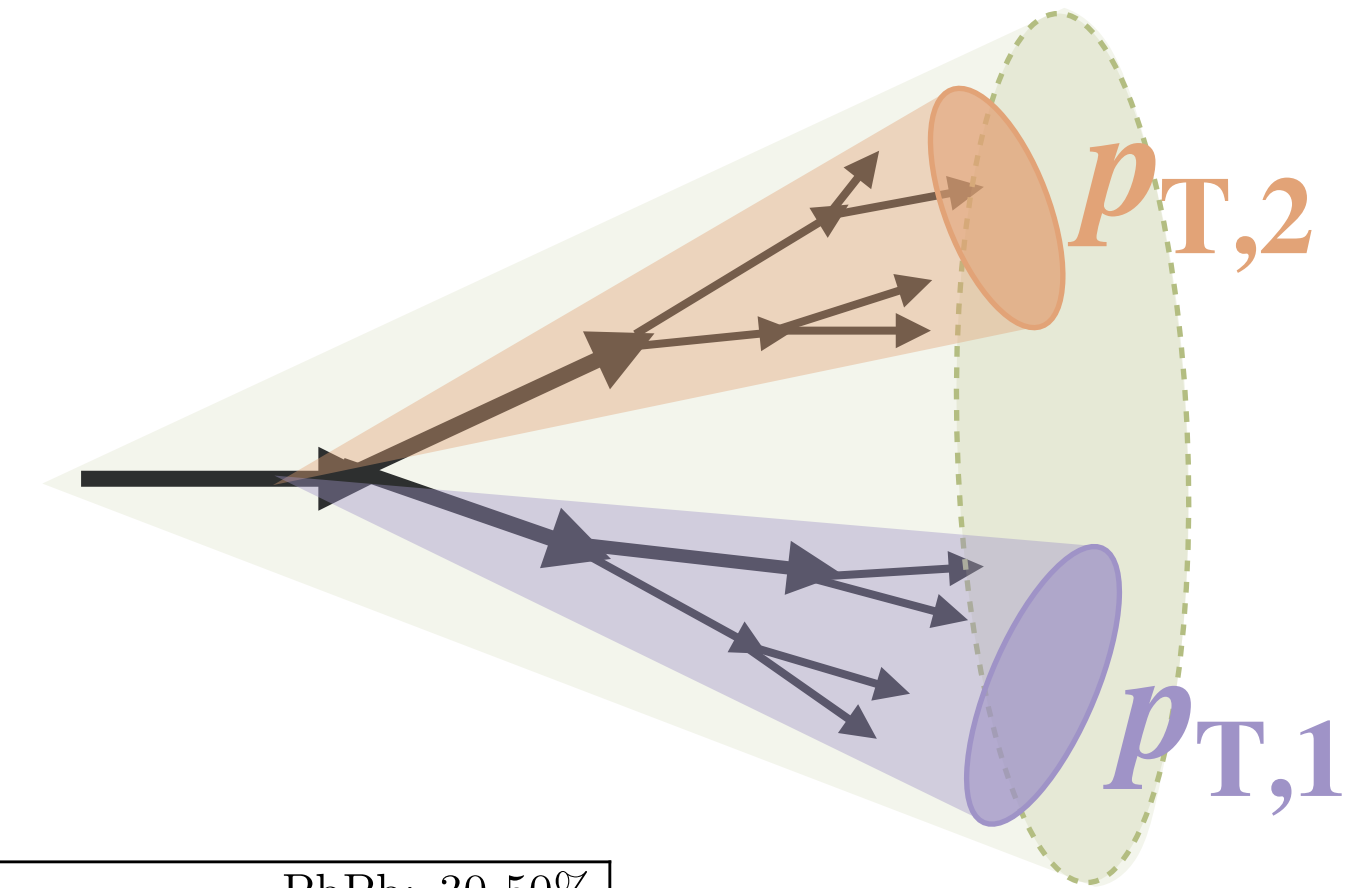
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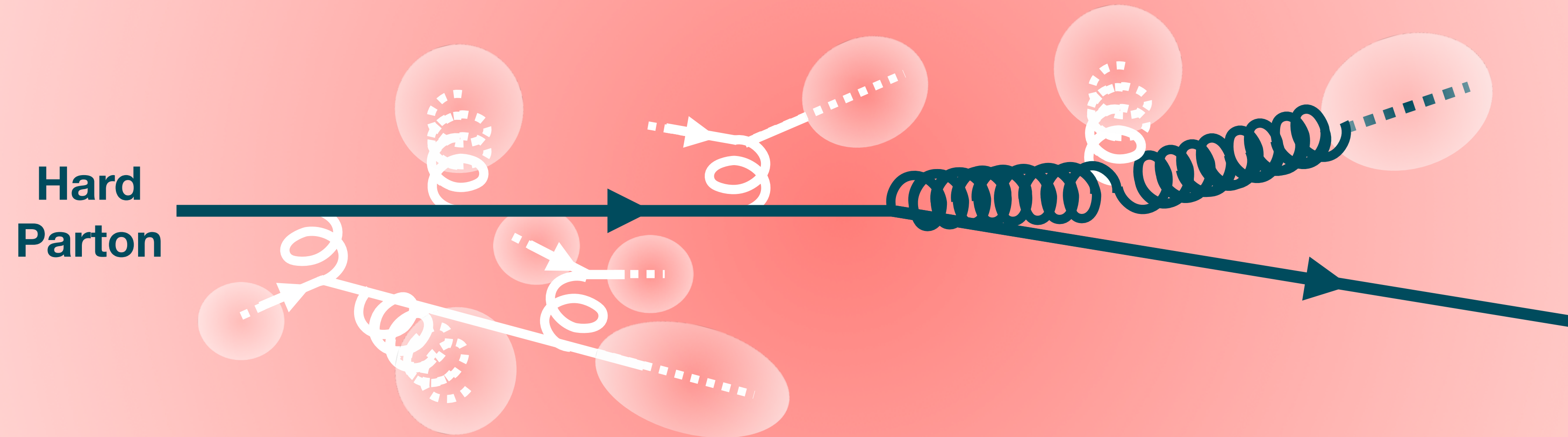
$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}}$$



- Good agreement with experimental data
- Almost no medium modification in hardest splittings

Fluid + Jet Approach for Hydro Response

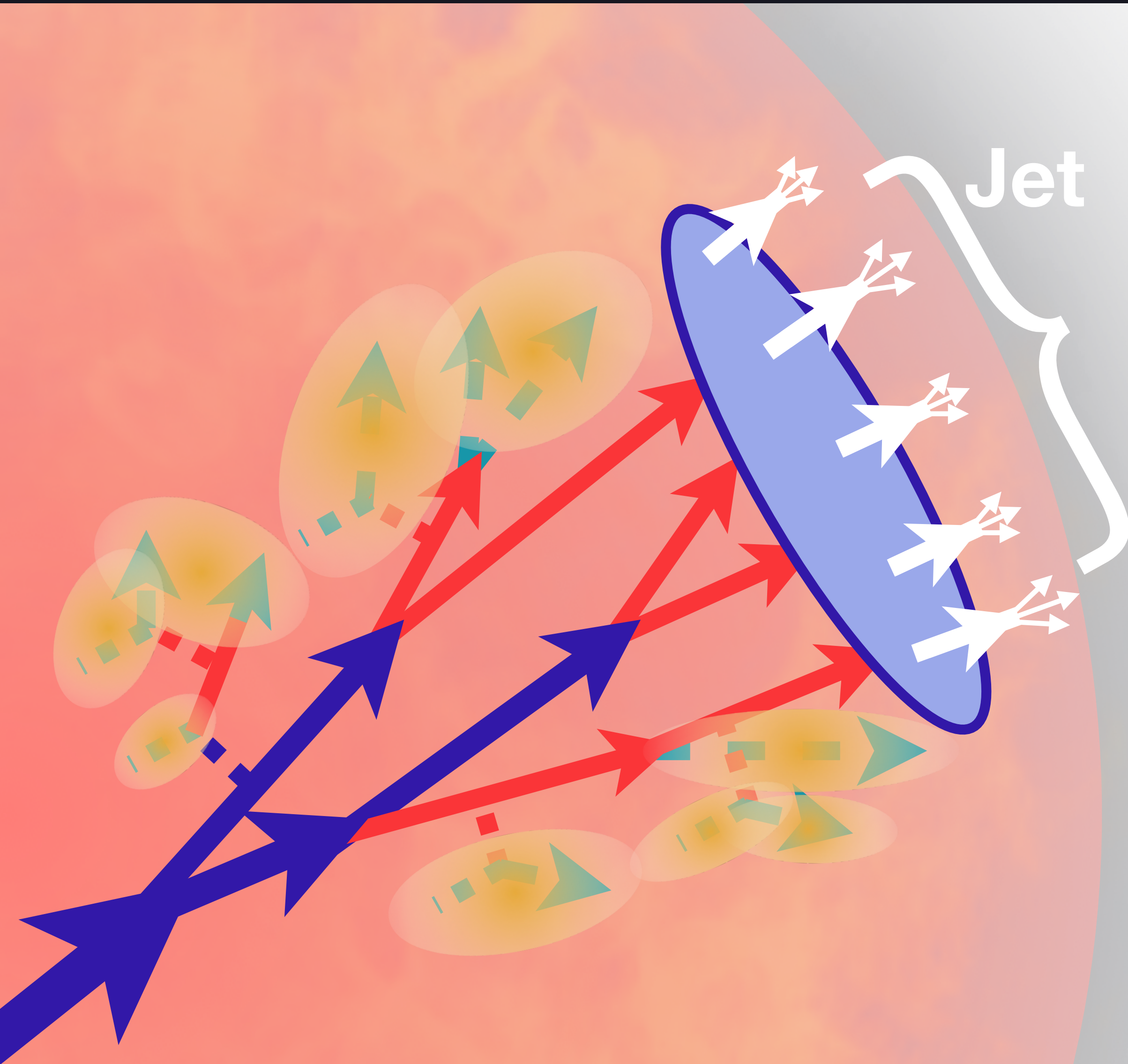
Hydrodynamic Medium Response to Hard Partons



- **In-medium thermalization**

- Drop to typical scale of thermalized medium constituents ($E \sim E_{\text{med}}$)
- Transition to hydrodynamic transport \rightarrow Hydrodynamic medium response

Hydrodynamic Medium Response Effect on Jets



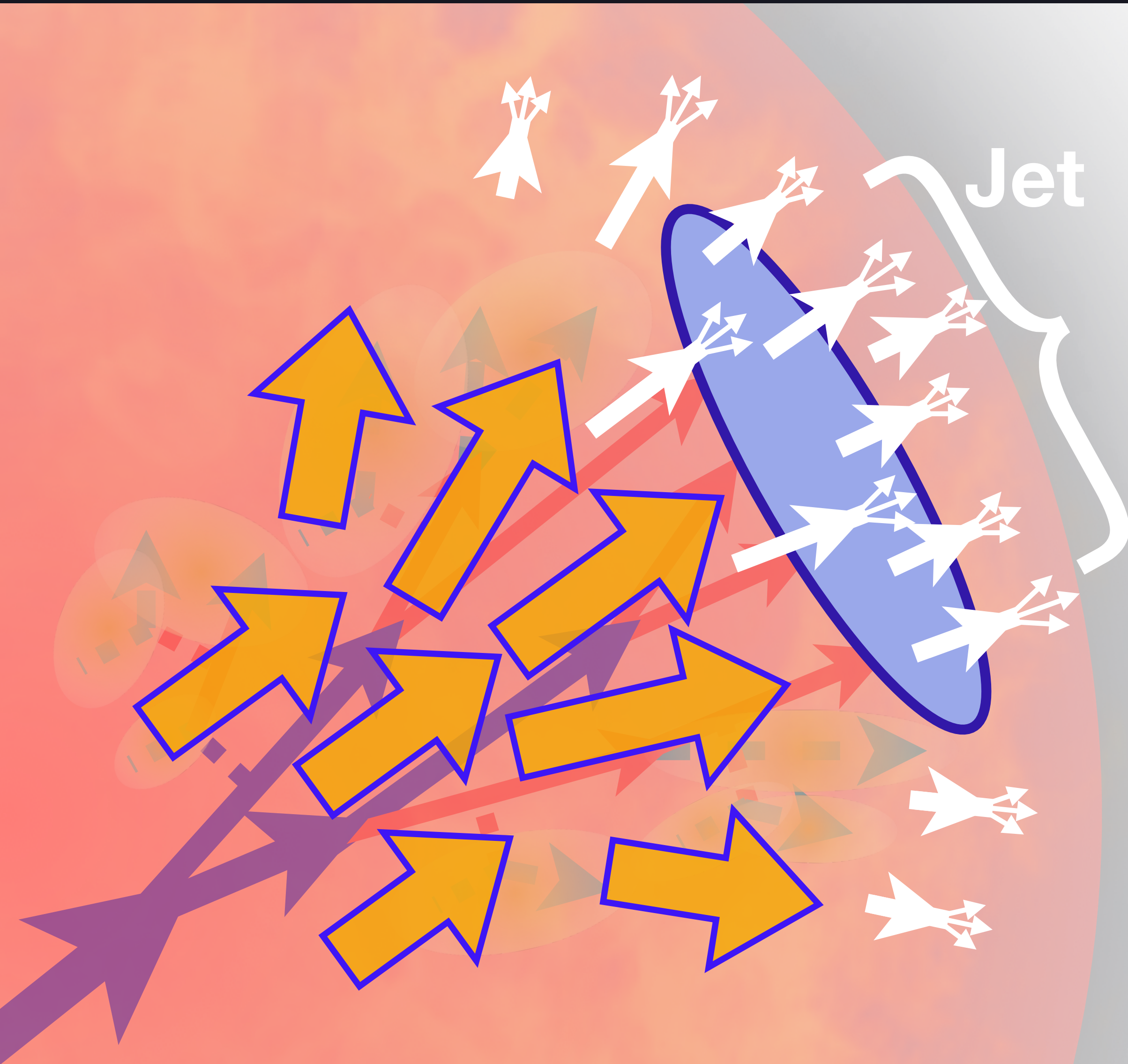
- **Jet-induced flow in medium**

- Transport momentum deposited by jet
- Modify particle emission around jet

- **Hydro medium response contribution**

- Soft, spread out from jet
- Jet-correlated, cannot be subtracted
- Affect structures inside/around jet

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Description of Hydro Medium Response to Jets

- **Medium fluid evolution with energy-momentum deposition**

Coupled Jet-Fluid (YT, N.-B. Chang, G.-Y. Qin), CoLBT-hydro (W. Chen, X.-N. Wang, W. Zhao,...)
EPOS3-HQ (I. Karpenko,...), JETSCAPE (JETSCAPE), Hybrid+Linearized Hydro (X. Yao, D. Pablos,...),
LEXUS+MUSIC (C. Shen, B. Schenke,...), DCCl2 (Y. Kanakubo, YT, T. Hirano,...), JAM (Y. Nara),...

- Hydrodynamic transport of jet energy-momentum via thermal partons
- Evolution together with the bulk QGP fluid

Hydrodynamic equation with source term

$$\nabla_{\mu} T^{\mu\nu}_{\text{med}}(\mathbf{x}) = J^{\nu}_{\text{jet}}(\mathbf{x})$$

Energy-momentum tensor
of the QGP fluid

Energy and momentum
deposited into the fluid

- Source term J^{ν}_{jet} constructed from jet-shower evolution calculation
- Bulk part particle with hydro response obtained via the Cooper-Frye

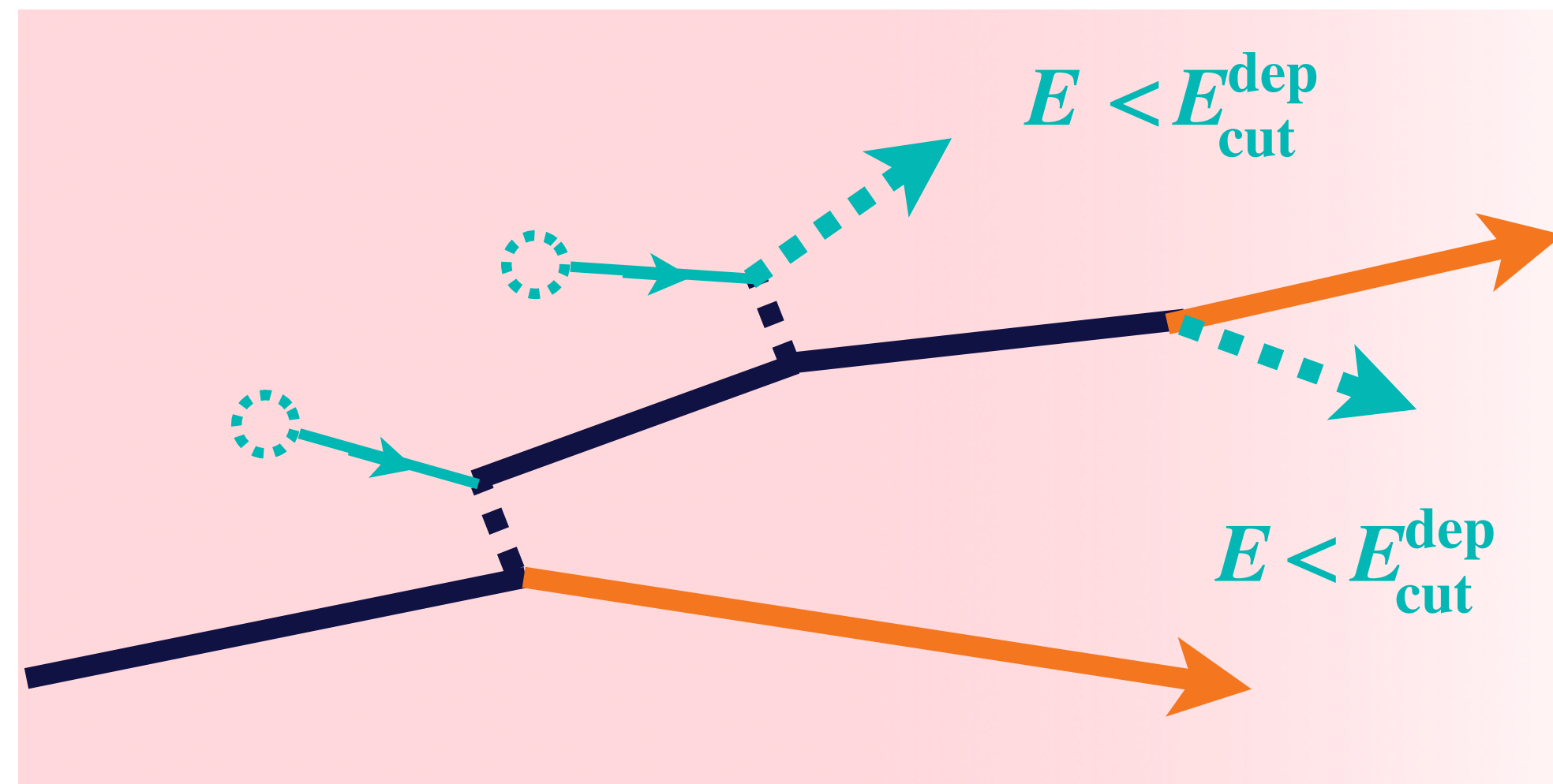
Causal Formulation for Source Term

YT, C. Shen and A. Majumder, arXiv:2001.08321

● Energy-momentum deposition

CoLBT-hydro (W. Chen, X.-N. Wang *et al.*)

- Soft partons
- Holes



$E_{\text{cut}}^{\text{dep}}$: Energy scale for in-medium thermalization

● Causal source profile

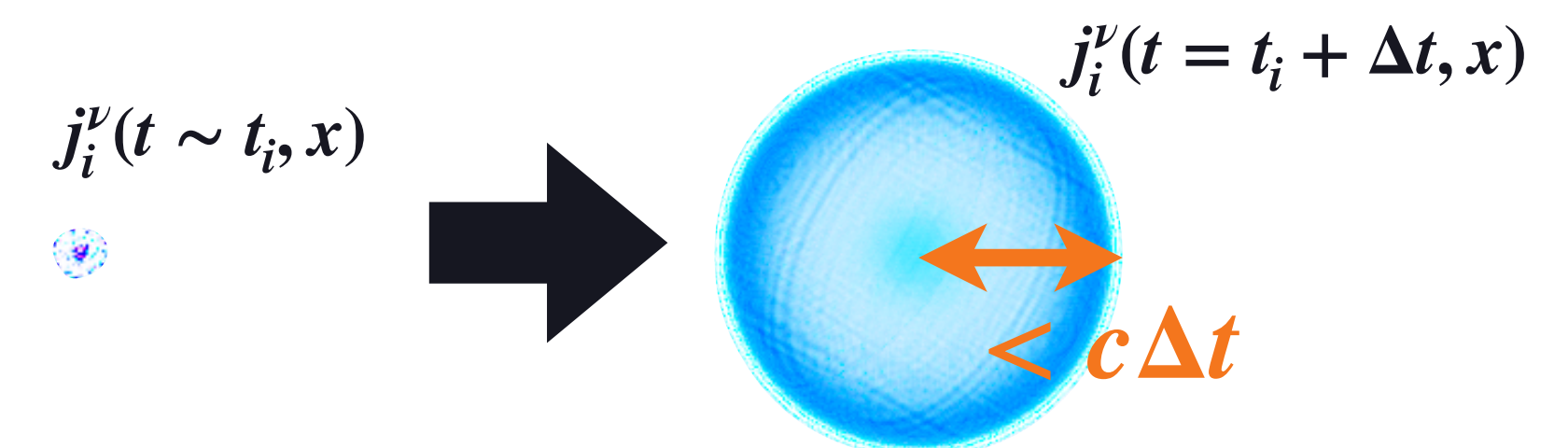
JETSCAPE (JETSCAPE)

- Relativistic diffusion equation

$$\left[\frac{\partial}{\partial t} + \tau_{\text{diff}} \frac{\partial^2}{\partial t^2} - D_{\text{diff}} \nabla^2 \right] j^\nu(\mathbf{x}) = 0$$

with initial condition

$$j^\nu(t = t_{\text{dep}}, \vec{x}) = p_{\text{dep}}^\nu \delta^{(3)}(\vec{x} - \vec{x}_{\text{dep}})$$



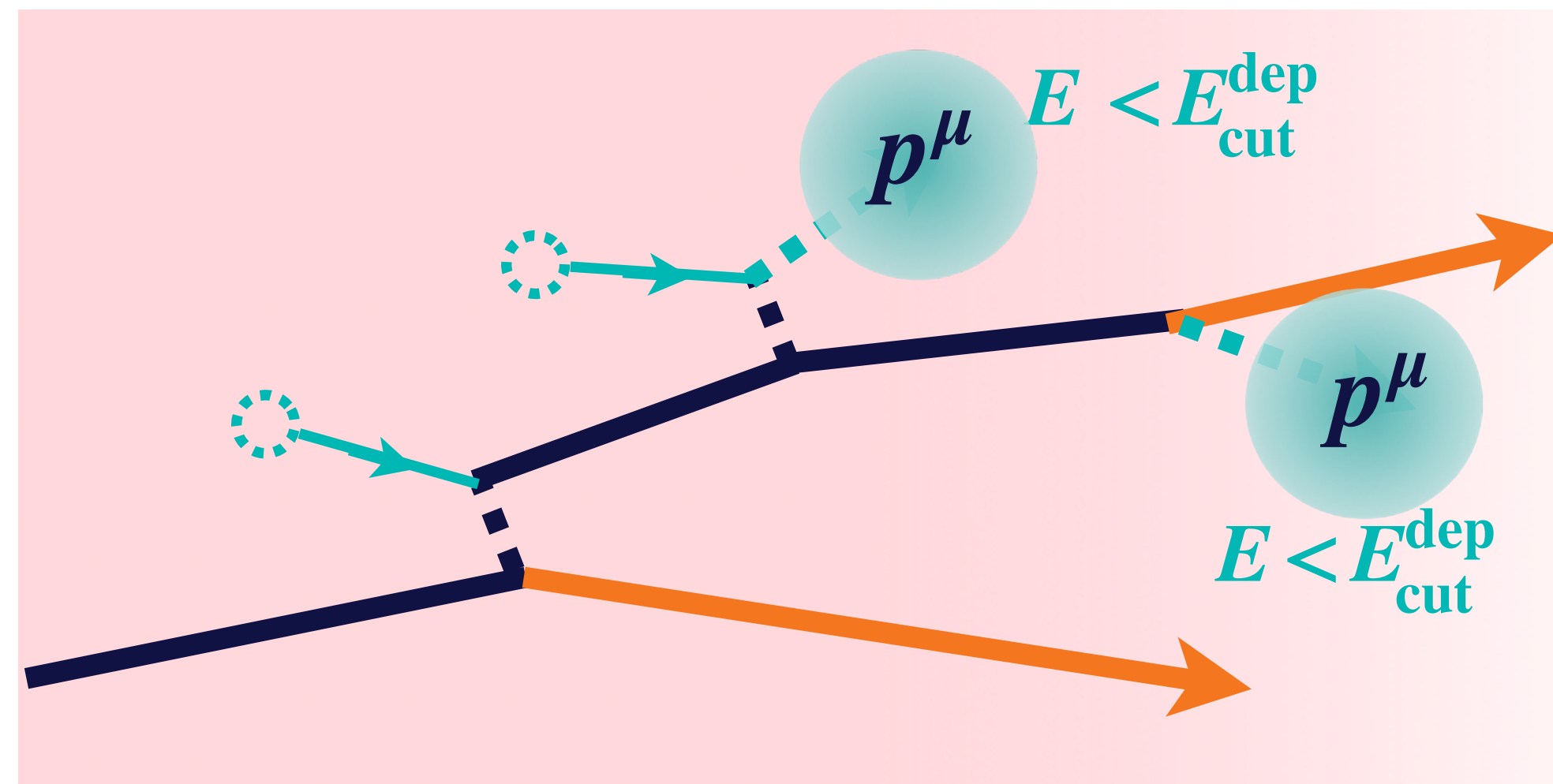
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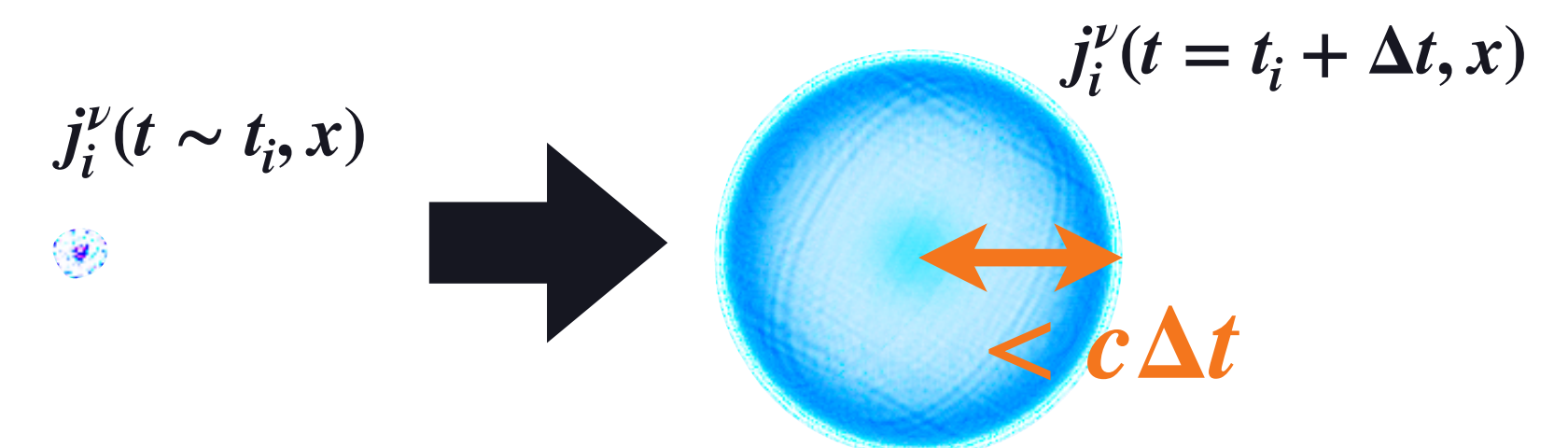
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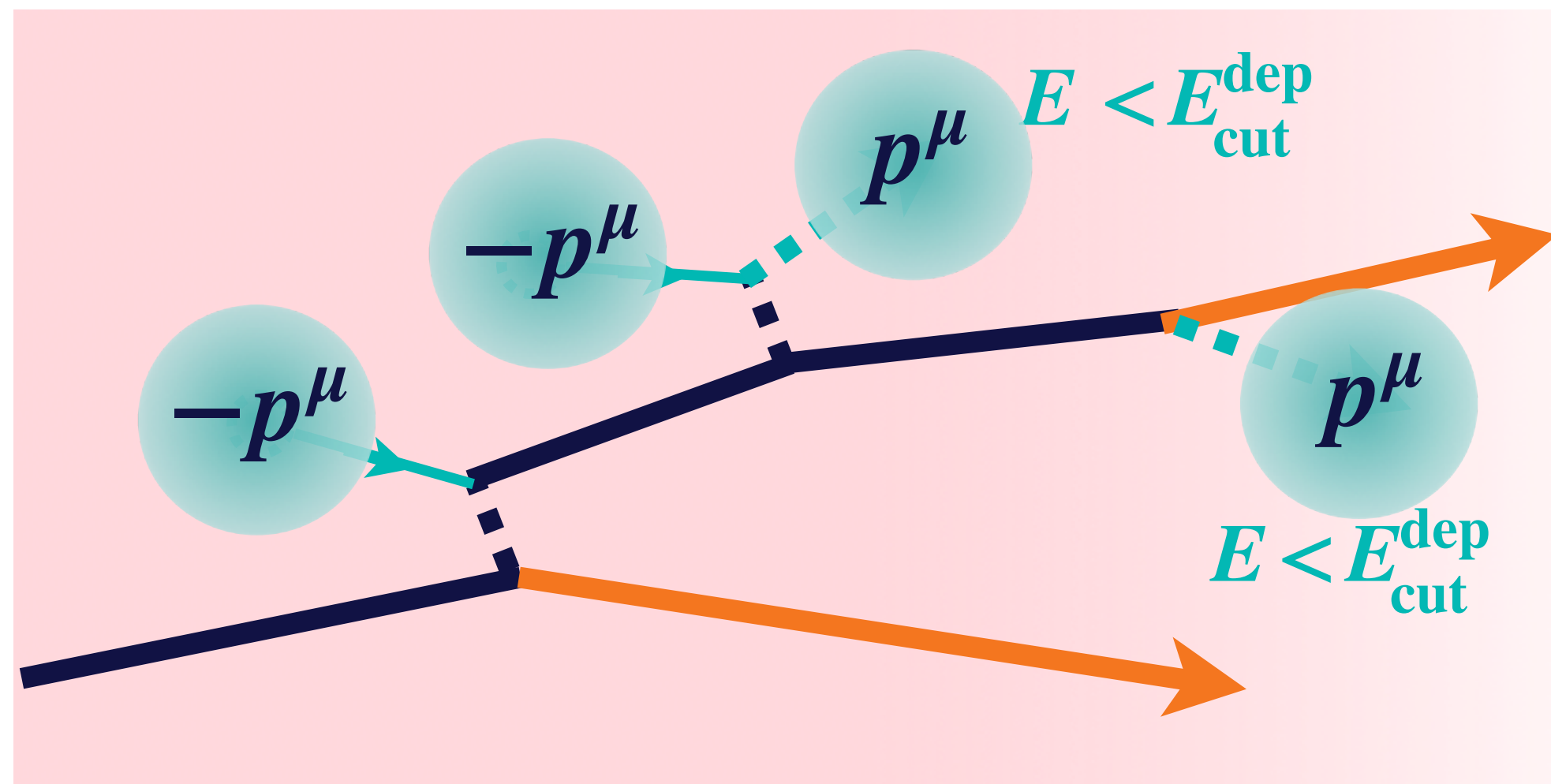
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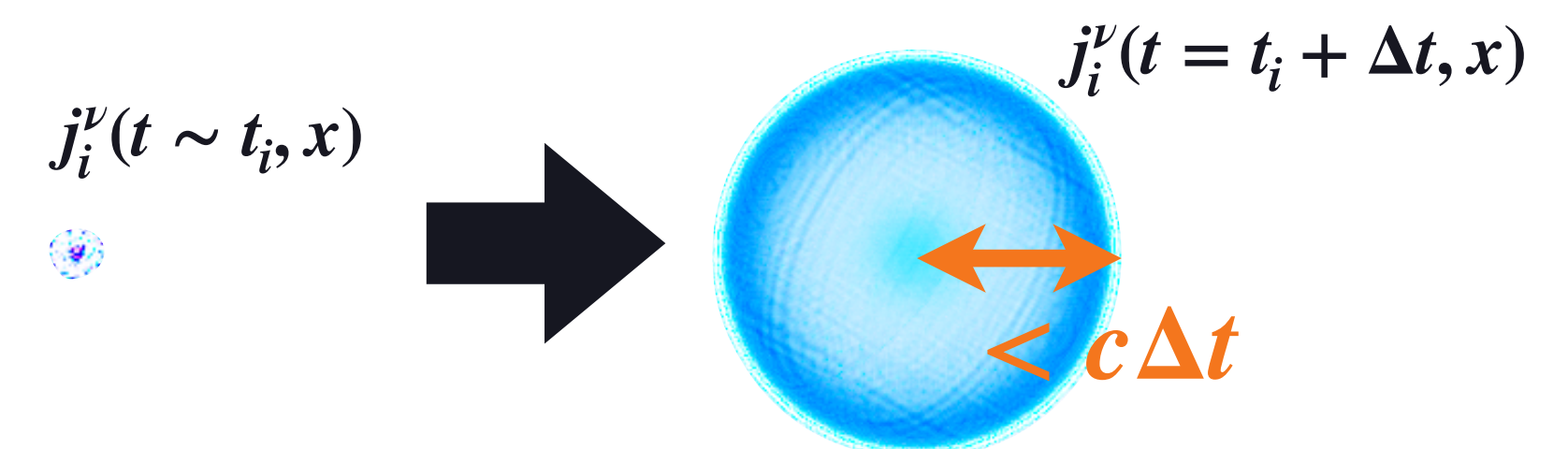
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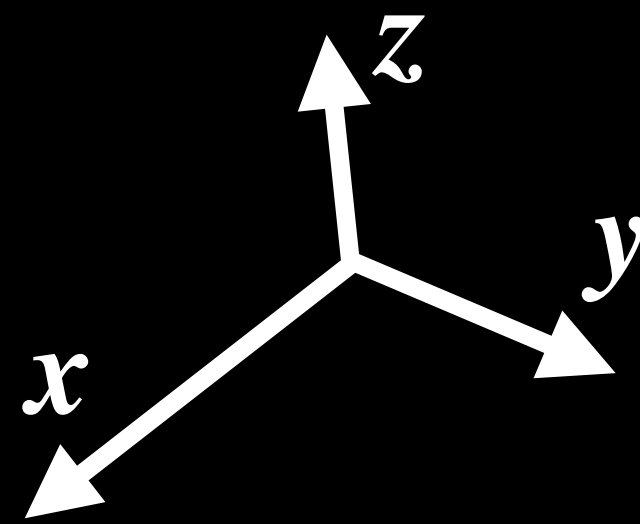


Evolution of Hydrodynamic Medium Response

MATTER + LBT + Causal Diff. + Ideal Hydro [Static Brick, $T_{\text{brick}} = 250 \text{ MeV}$]

YT, C. Shen, A. Majumder, arXiv:2001.08321

- Jet-Induced flow induced by a parton shower propagating in the x direction



Orange: Region with $T > 250 \text{ MeV}$

Blue: Region with $T < 250 \text{ MeV}$

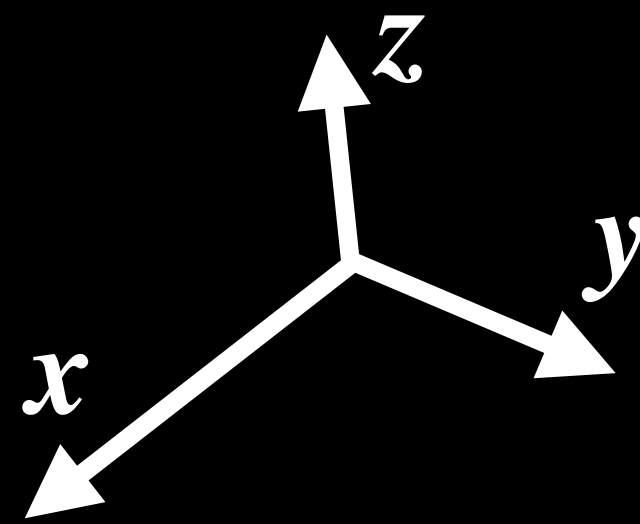
Red: Energetic Partons

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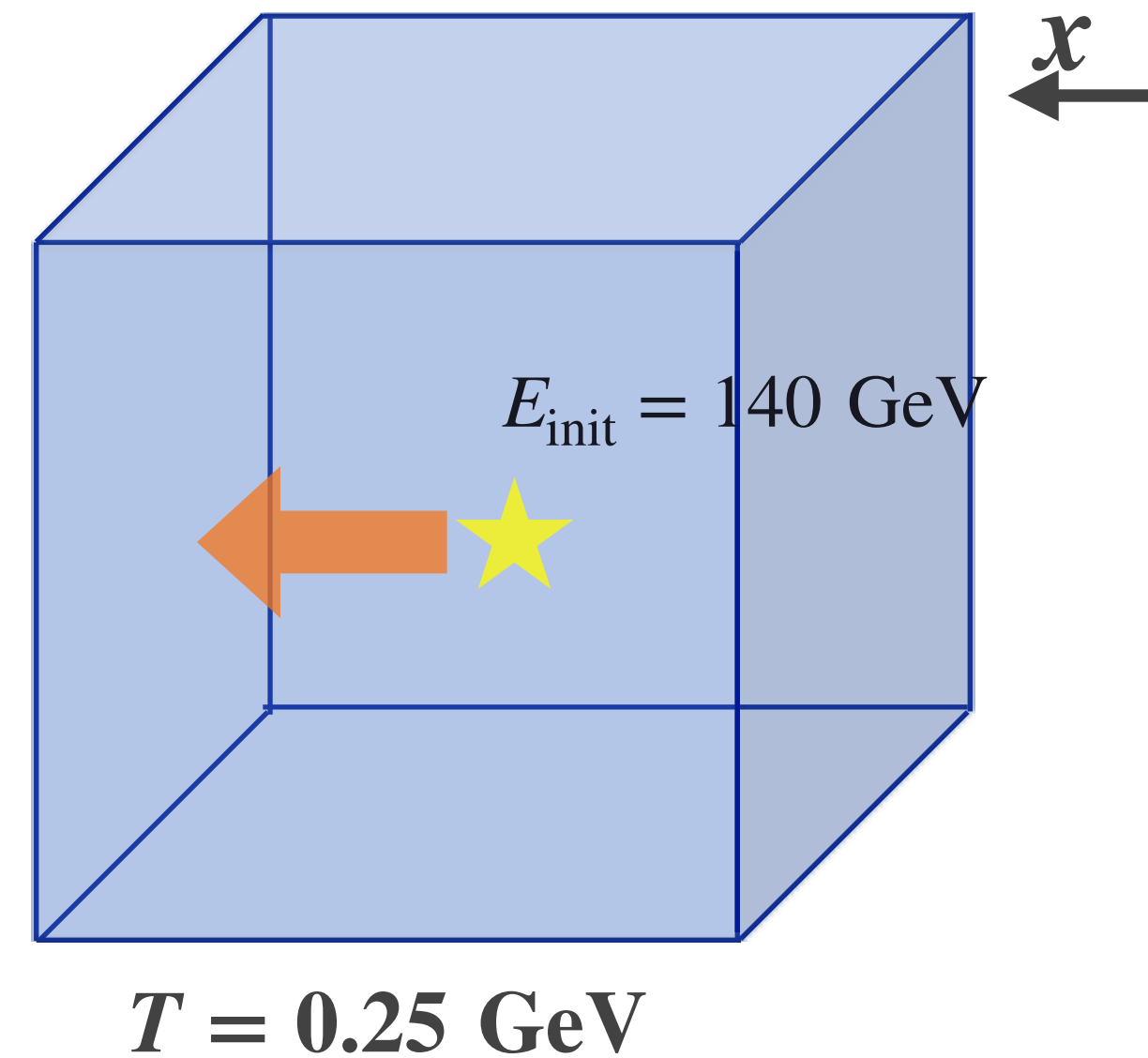
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Recoil vs Recoil+Hydro response: Static brick case

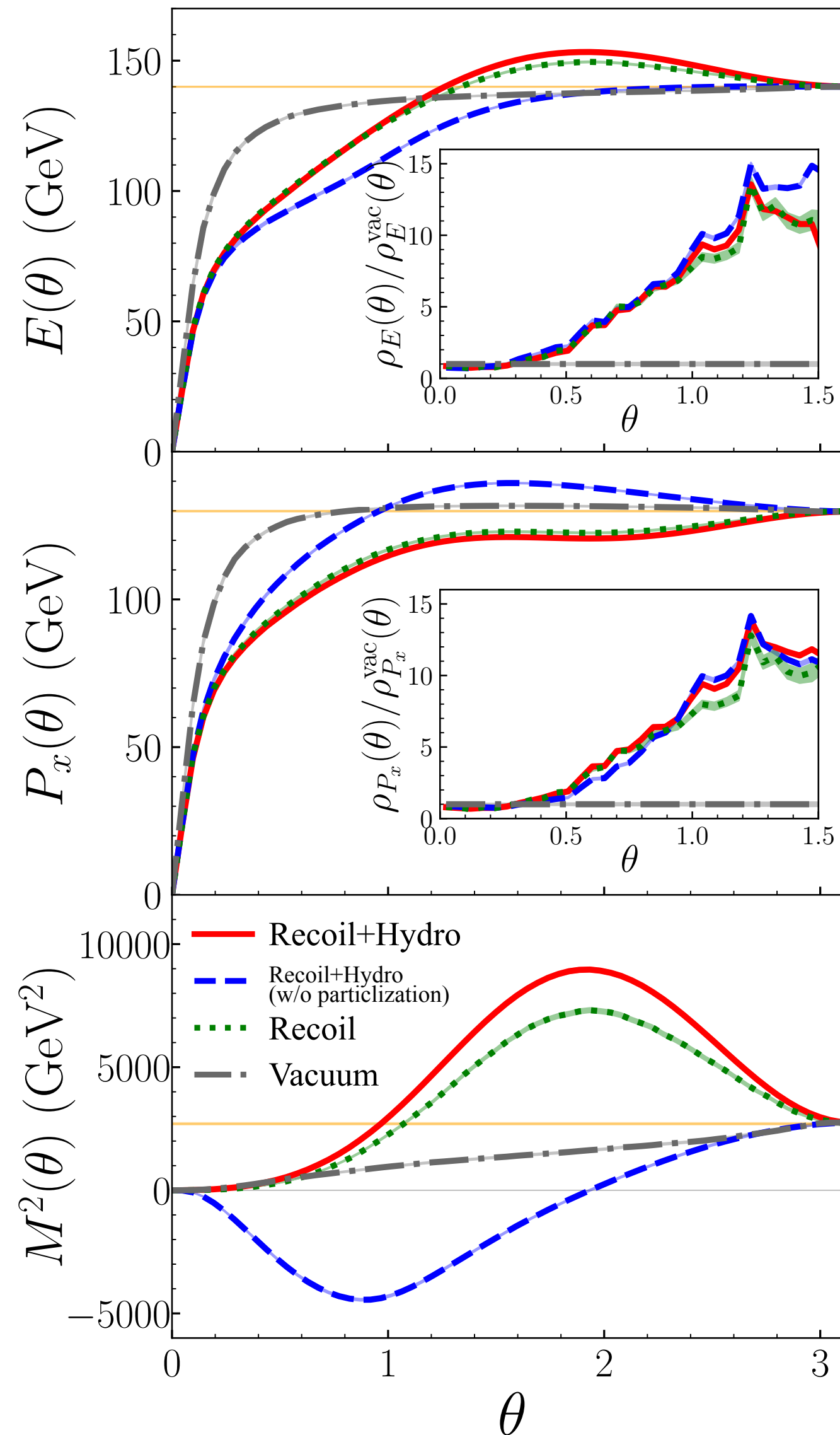
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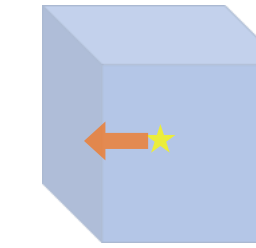
- Jet propagation in medium with static uniform initial condition
- Energy loss by MATTER+LBT with recoils
- Medium evolves upto $t = 10 \text{ fm}$

Recoil vs Recoil+Hydro response: Static brick case

YT, C. Shen and A. Majumder, arXiv:2001.08321

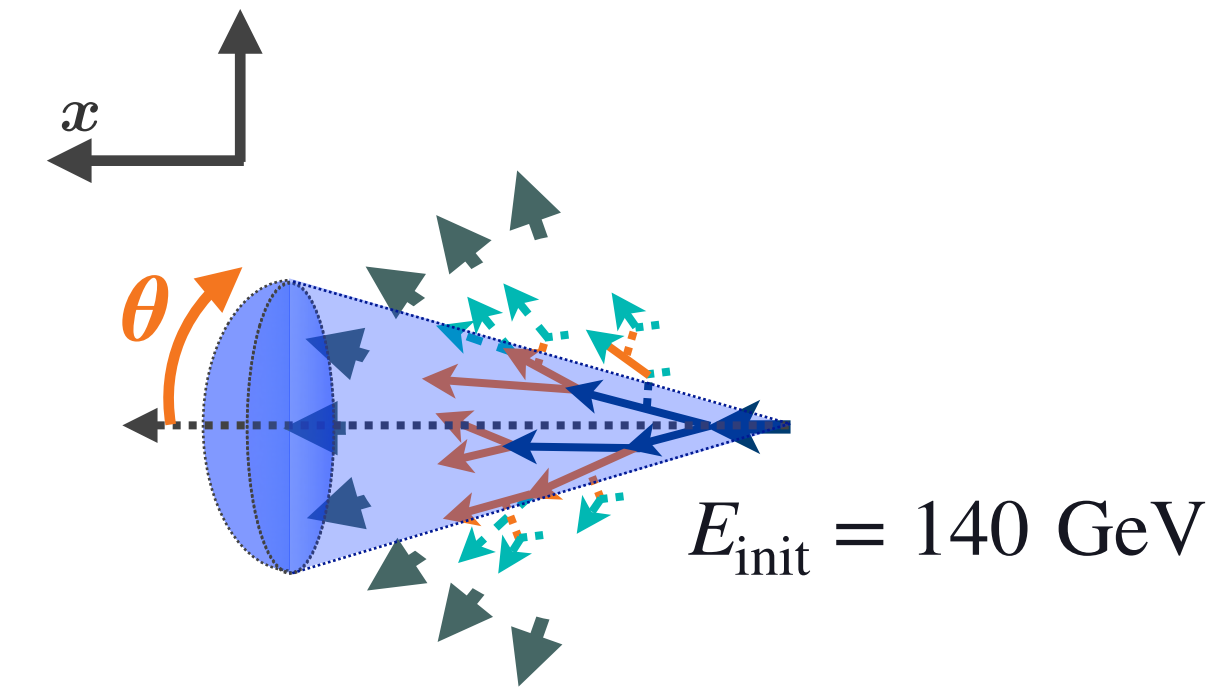


Angular structure of jet in brick



- Jet energy, momentum and mass

$$P^\mu(\theta) = \int_0^\theta d\theta' \frac{dP^\mu}{d\theta'}, \quad M^2(\theta) = P^\mu(\theta)P_\mu(\theta)$$



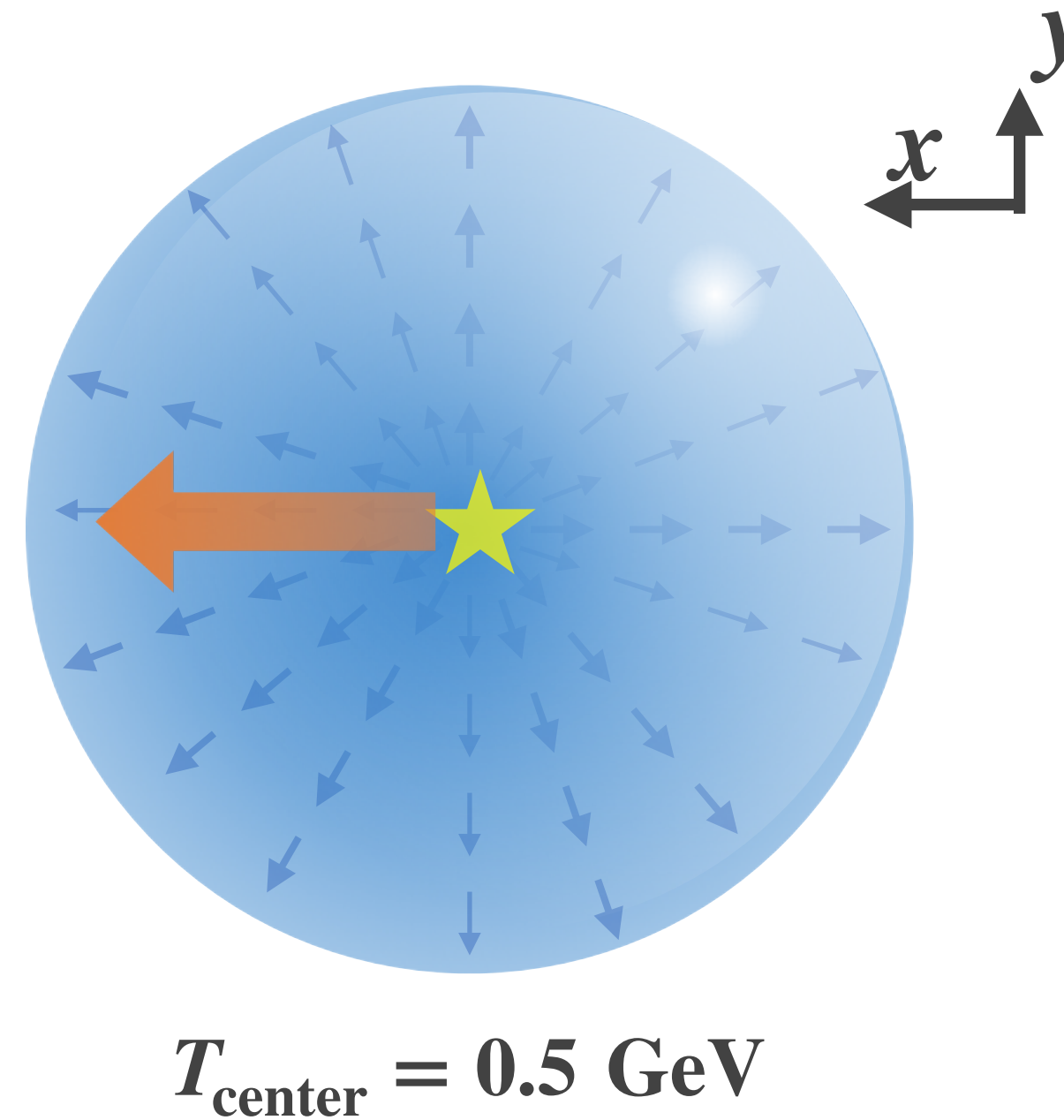
- Detailed substructure

$$\rho_E(\theta) = \frac{1}{E(\theta=1)} \frac{dE}{d\theta}, \quad \rho_{P_x}(\theta) = \frac{1}{P_x(\theta=1)} \frac{dP_x}{d\theta}$$

- Backward suppression due to particlization (**Recoil+Hydro**)
- Backward suppression due to holes (**Recoil**)

Recoil vs Recoil+Hydro response: Expanding medium case

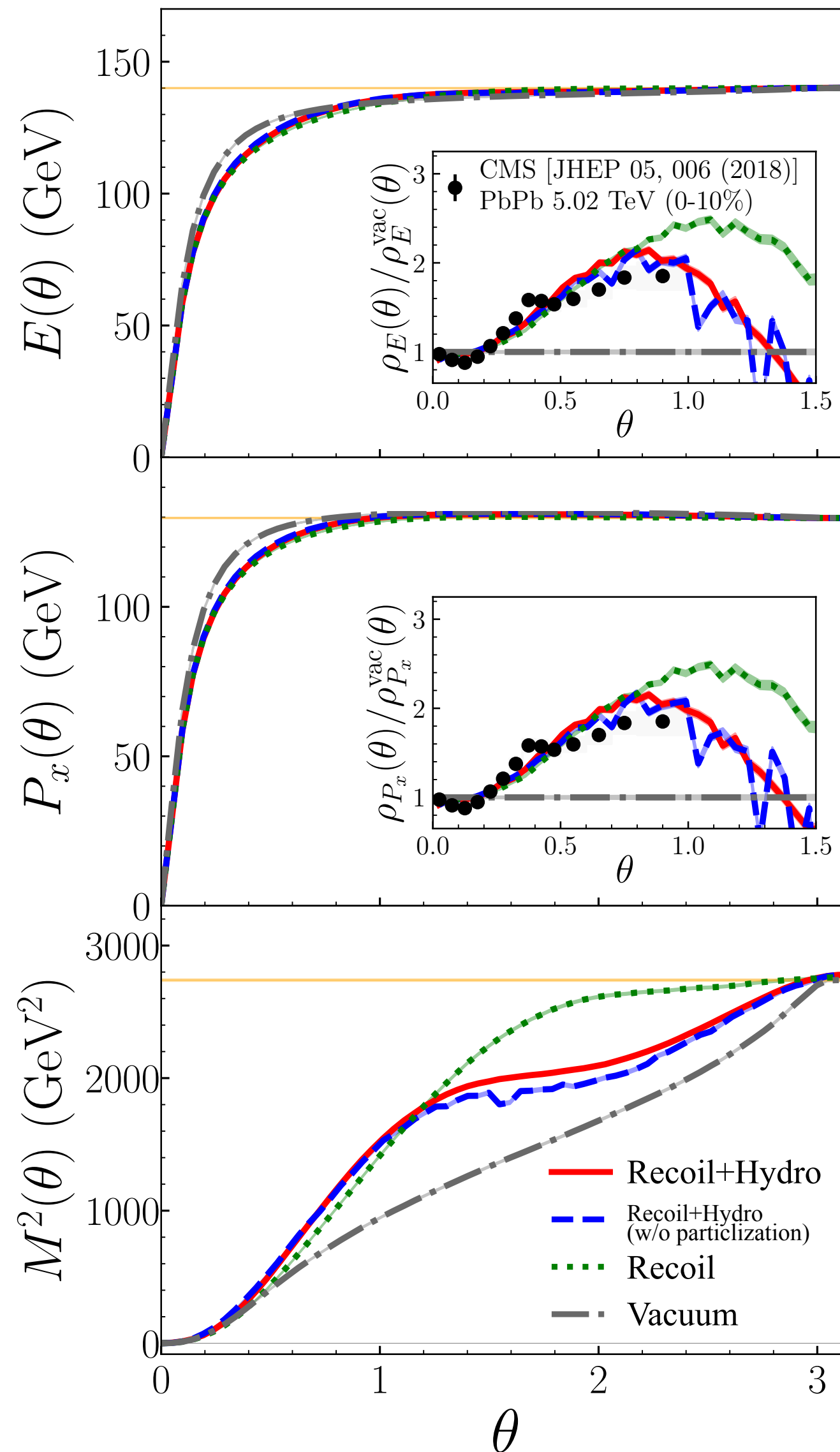
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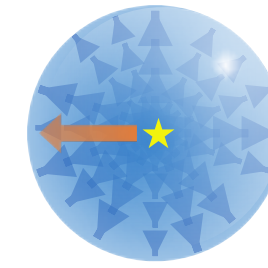
- Jet propagation in medium with oblate 3-D Gaussian ($\sigma_T = 1.5 \text{ fm}$, $\sigma_z = 0.75 \text{ fm}$)
- Medium size is chosen to reproduce the full simulation results
- Radial flow following the jet propagation

Recoil vs Recoil+Hydro response: Expanding medium case

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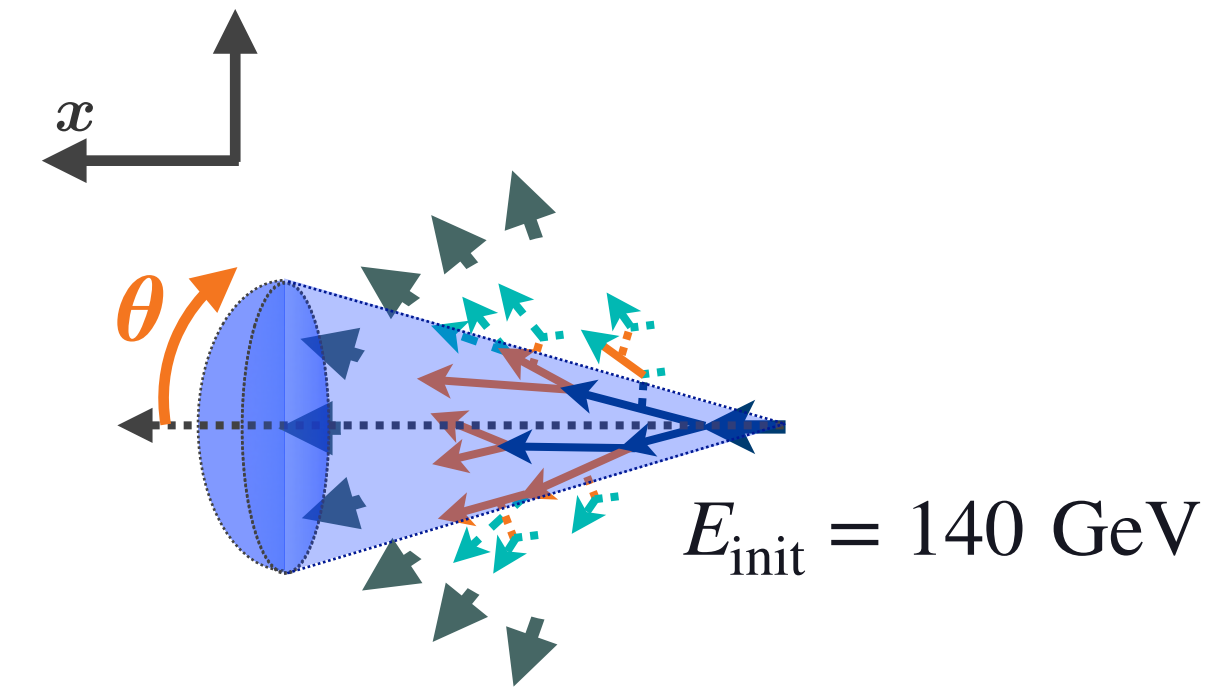


Angular structure of jet in oblate medium



- Jet energy, momentum and mass

$$P^\mu(\theta) = \int_0^\theta d\theta' \frac{dP^\mu}{d\theta'}, \quad M^2(\theta) = P^\mu(\theta)P_\mu(\theta)$$



- Detailed substructure

$$\rho_E(\theta) = \frac{1}{E(\theta=1)} \frac{dE}{d\theta}, \quad \rho_{P_x}(\theta) = \frac{1}{P_x(\theta=1)} \frac{dP_x}{d\theta}$$

- Collimation due to push by the radial flow
- Small effect of particlization (**Recoil+Hydro**)
- Clear difference at very large angle region ($\theta > 1$)

Summary

● Jet evolution in JETSCAPE

- Multi-stage description by switching modules with virtuality
- Further extension by Q^2 -dependence in jet quenching parameter \hat{q}
- Simultaneous description of jet and high- p_T particle energy loss in various $\sqrt{s_{NN}}$
- Further systematic studies for jet substructure

● Hydrodynamic medium response

- Transport of thermalized jet energy and momentum
- Described by hydrodynamic equation with source terms
- Difference from recoils led by background flow

Backup

Causal Formulation for Source Term

YT, C. Shen and A. Majumder, arXiv:2001.08321

